



**MEASUREMENTS AND CORRELATIONS OF TRANSITION  
REYNOLDS NUMBERS ON SHARP SLENDER  
CONES AT HIGH SPEEDS**

**S. R. Pate**

**ARO, Inc.**

**December 1969**

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## FOREWORD

The work reported herein was sponsored by Headquarters, Arnold Engineering Development Center (AEDC), Air Force Systems Command (AFSC), in support of Project 8953, Task 03, Program Element 62201F.

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This technical report has been reviewed and is approved.

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**ABSTRACT**

An experimental investigation of laminar boundary-layer transition on a sharp, 10-deg total-angle, insulated cone at zero yaw was conducted in the AEDC-VKF 12- and 40-in. supersonic wind tunnels at free-stream Mach numbers from 3 to 6. This research was directed toward defining the relationship between the aerodynamic noise disturbances and boundary-layer transition Reynolds numbers  $(Re_t)_\delta$  in high-speed wind tunnels and has extended previously published planar results to include axisymmetric models. A significant increase in  $(Re_t)_\delta$  with increasing tunnel size (similar to the planar results) is shown to exist. Sharp cone transition Reynolds numbers from ten facilities (12- to 54-in.) for free-stream Mach numbers from 3 to 14 and a unit Reynolds number per inch range from  $0.1 \times 10^6$  to  $1.2 \times 10^6$  have been correlated using aerodynamic-noise-transition parameters. A quantitative correlation of the ratio between cone and planar  $(Re_t)_\delta$  values has been developed which demonstrates a strong Mach number dependence and also indicates a variation with tunnel size and unit Reynolds number.

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## NOMENCLATURE

$b$	Model nose bluntness, in.
$C_F$	Mean turbulent skin friction coefficient
$c$	Tunnel test section circumference, in.
$c_1$	Tunnel test section circumference of 12- by 12-in. tunnel ( $c_1 = 48$ in.)
$\ell_m$	Axial distance from tunnel throat to model nose, in.

$\ell_r$	Axial distance from tunnel throat to wall boundary-layer rake, in.
$M$	Mach number
$p$	Surface probe pitot pressure, psia
$p_c$	Cone surface static pressure, psia
$p_o$	Tunnel stilling chamber pressure, psia
$p_o'$	Total pressure downstream of a normal shock wave at free-stream conditions, psia
$\tilde{p}$	Root-mean-square of pressure fluctuation, psia
$p_\infty$	Free-stream static pressure, psia
$q_\infty$	Free-stream dynamic pressure, psia
$\dot{q}$	Heat-transfer rate, Btu/ft <sup>2</sup> -sec
$(Re_t)_\delta$	Transition Reynolds number (based on local conditions), $(Re_t)_\delta = (Re/in.)_\delta x_t$
$Re_\delta$ or $(Re/in.)_\delta$	Inviscid flow local surface unit Reynolds number per inch, $U_\delta/\nu_\delta$
$Re_\infty$ or $(Re/in.)_\infty$	Free-stream Reynolds number per inch, $U_\infty/\nu_\delta$
$T$	Static temperature, °R or °F
$T_o$	Tunnel stilling chamber total temperature, °R or °F
$U$	Velocity, ft/sec
$x$	Surface distance measured from cone apex, in.
$x_t$	Surface distance location of boundary-layer transition, in.
$\delta^*$	Boundary-layer displacement thickness (tunnel wall), in.
$\theta_c$	Cone half-angle, deg
$\mu$	Absolute viscosity, lb-sec/ft <sup>2</sup>
$\nu$	Kinematic viscosity, in.-ft/sec

#### SUBSCRIPTS

aw	Adiabatic wall
c	Cone configuration



planar	Two-dimensional configuration, either hollow cylinder or flat plate
w	Wall
$\delta$	Local inviscid flow properties
$\infty$	Free-stream

## SECTION I INTRODUCTION

Whenever theoretical analyses for a particularly difficult, but equally important, physical phenomenon are known to be inadequate then solutions must, from necessity, be provided by experimental and empirical results. For over six decades the laminar boundary-layer transition process has defied the development of a successful theoretical analysis. Consequently, the bulk of the knowledge accumulated to date on this very complex fluid flow phenomenon has relied almost entirely on experimental data. Unfortunately, however, as experimentalists continue to gather transition data — to advance the state of the art and to meet the demands dictated by high performance reentry vehicles and supersonic-hypersonic cruise aircraft — it is becoming more evident that the transition process (as was the case with the now historic stability experiments of Ref. 1) is critically dependent, even at supersonic-hypersonic Mach numbers, on the free-stream disturbance modes present in conventional experimental facilities.

Facility-generated disturbances (primarily vorticity) present in subsonic and low supersonic ( $M_\infty \leq 3$ ) wind tunnels have long been recognized to have a significant and adverse effect on transition, Refs. 1 through 7. However, for lack of evidence it has been the policy of most transition investigators to assume that the disturbance modes present at higher Mach numbers ( $M_\infty \geq 3$ ) (primarily radiated sound or aerodynamic noise) had negligible effects on the location of transition and on the development of the transition process.

However, recent experimental transition research by Pate and Schueler, Refs. 8 and 9, has shown, conclusively, the severe, adverse effect that the aerodynamic noise which radiates from the turbulent boundary layer on the walls of supersonic and hypersonic tunnels will have on transition. These studies have provided an extensive and unique aerodynamic-noise-transition Reynolds number correlation of high-speed ( $3 \leq M_\infty \leq 8$ ) wind tunnel  $(Re_t)_\delta$  data from many different facilities. The intensity of the radiated noise as reported in Refs. 8 and 9 was related to the tunnel size, tunnel wall boundary-layer state (laminar, transitional, or turbulent), tunnel unit Reynolds number, and tunnel Mach number.

Over the years, experimentalists have attempted to establish a valid relationship between cone and flat plate transition Reynolds numbers. Perhaps the most significant results to date in this area were those reported in Refs. 10 and 11. From a qualitative comparison of  $(Re_t)_\delta$  data obtained on axisymmetric and planar models from several sources and several different wind tunnels, Potter and Whitfield, Ref. 10, observed

that the  $(Re_t)_\delta$  ratio (cone to planar) appeared to decrease from a value of approximately three at  $M_\delta = 3$  to about one near  $M_\delta = 8$ . However, more recently in Ref. 11, Whitfield and Iannuzzi concluded that attempts at direct comparison of cone and planar  $(Re_t)_\delta$  data from various high-speed facilities must now be viewed with reservation and that cone-planar  $(Re_t)_\delta$  ratio results cannot be clearly established from presently available experimental data. Their conclusions were based primarily on the recent transition studies of Pate and Schueler, Refs. 8 and 9. Therefore, evidence to date appears to indicate that the free-stream disturbances present in high-speed test facilities are also masking the factor of three difference between cone and flat plate  $(Re_t)_\delta$  values that have been reported experimentally and implied by many investigators using the theoretical analysis of Tetervin in Ref. 12.

The purpose of this research was to extend the investigation of tunnel aerodynamic noise effects on transition to include axisymmetric models. Slender cone models have been tested at  $3 \leq M_\infty \leq 6$  to determine if cone transition Reynolds numbers varied appreciably with the tunnel size and to establish if an aerodynamic-noise-transition correlation similar to the planar results of Refs. 8 and 9 could be developed.

These transition studies, conducted in the Tunnels A and D (Gas Dynamic Wind Tunnels, Supersonic (A) and (D), respectively), have also provided new information on the relation between cone and flat plate (planar) transition Reynolds numbers obtained in high-speed ( $3 \leq M_\infty \leq 8$ ), conventional wind tunnels.

## SECTION II EXPERIMENTAL CONDITIONS

### 2.1 WIND TUNNEL FACILITIES

New experimental data included in this report were obtained at the Arnold Engineering Development Center (AEDC) in the von Kármán Gas Dynamics Facility (VKF), supersonic Tunnels A and D.

#### 2.1.1 Tunnel D

Tunnel D is an intermittent, variable density wind tunnel with a manually adjusted, flexible-plate-type nozzle and a 12- by 12-in. test section. The tunnel operates at Mach numbers from 1.5 to 5 at stagnation pressures from about 5 to 60 psia, respectively, and at average stagnation temperatures of about 70°F.

### 2.1.2 Tunnel A

Tunnel A is a continuous, closed-circuit, variable density wind tunnel with an automatically driven, flexible-plate-type nozzle and a 40- by 40-in. test section. The tunnel operates at Mach numbers from 1.5 to 6 at maximum stagnation pressures from 29 to 200 psia, respectively, and stagnation temperatures up to 290°F ( $M_\infty = 6$ ). Minimum operating pressures range from about one-tenth to one-twentieth of the maximum pressures.

## 2.2 TRANSITION MODELS AND APPARATUS

The transition model, Figs. 1 and 2 (Appendix I), was a 10-deg total-angle, stainless steel cone equipped with a tool steel nose section. The model had a surface finish of approximately 10  $\mu$ in. and a tip bluntness (b) between 0.005 and 0.006 in. The Tunnel D model consisted of the nose and center section as shown in Fig. 1. The Tunnel A model was obtained by adding an aft section as shown in Figs. 1 and 2. In order to maintain a near-perfect joint between the sections, the model surface was refinished after attaching each model section.

A remotely controlled, electrically driven, surface pitot probe (tip geometry illustrated in Fig. 1a) as shown in Figs. 1b and 2 provided a continuous trace of the probe pressure on an X-Y plotter from which the location of transition was determined.

Schlieren and shadowgraph photographic systems were used as a secondary method for detecting the location of transition in Tunnels D and A, respectively.

A 1/4-in.-diam, flush-mounted surface microphone having a frequency response from 0 to 30 kHz and a dynamic response from 70 to 180 db was also used to measure the model surface pressure fluctuations in the laminar, transitional, and turbulent flow regimes and to determine the location of transition.

## SECTION III INVISCID FLOW CONE PROPERTIES

The unit Reynolds number ratios at the surface of sharp, unyawed cones, assuming inviscid flow properties, have been calculated and the results are presented in Fig. 3. The justification for presenting these

results was precipitated by the fact that in reviewing published transition results it became apparent that inconsistencies existed in the calculation of tunnel unit Reynolds numbers and more often for cone surface values. These differences were traceable primarily to the different viscosity relationships used. Therefore, the surface Reynolds number ratios assuming inviscid flow over sharp, unyawed cones were calculated using three different methods.

1. Using the linear viscosity law ( $\mu \approx T$ ) which is valid for temperatures below approximately 216°R.

$$\left[ \frac{(\text{Re}\delta)_c}{\text{Re}_\infty} \right]_{\text{linear law}} = \frac{p_c}{p_\infty} \frac{M_c}{M_\infty} \left( \frac{T_\infty}{T_c} \right)^{1.5} \quad (1)$$

2. Using Sutherland's viscosity law which is valid for temperatures above approximately 216°R.

$$\left[ \frac{(\text{Re}\delta)_c}{\text{Re}_\infty} \right]_{\text{Sutherland}} = \frac{p_c}{p_\infty} \frac{M_c}{M_\infty} \left( \frac{T_\infty}{T_c} \right)^2 \left( \frac{T_c + 198.6}{T_\infty + 198.6} \right) \quad (2)$$

3. Using a combination of the linear and Sutherland viscosity laws

$$\left[ \frac{(\text{Re}\delta)_c}{\text{Re}_\infty} \right]_{\substack{\text{linear} \\ \text{plus Sutherland}}} = \frac{p_c}{p_\infty} \frac{M_c}{M_\infty} \left( \frac{T_\infty}{T_c} \right)^{\frac{1}{2}} \frac{\mu_\infty}{\mu_c} \quad (3)$$

for  $T \leq 215^\circ\text{R}$ ,  $(\mu)_{\text{linear}} = (0.0805 \times 10^{-8}) (T)$ , lb-sec/ft<sup>2</sup>

$T \geq 216^\circ\text{R}$ ,  $(\mu)_{\text{Sutherland}} = \frac{2.270 \times (T)^{1.5}}{198.6 + T} \times 10^{-8}$ , lb-sec/ft<sup>2</sup>

Equation (3) combines the two viscosity laws and thus provides the more general method for calculating the Reynolds number ratio. A combination of the viscosity laws allows the free-stream viscosity to be determined using the linear law and the cone surface value to be evaluated using the Sutherland law which is often the condition existing in wind tunnels at high supersonic and hypersonic Mach numbers.

Figure 3a presents the Reynolds number ratios for  $M_\infty = 2, 5$ , and 12 and cone half-angles ( $\theta_c$ ) from 0 to 35 deg. As clearly evident, the three methods can produce significant differences depending on the combined effects of cone angle and flow conditions.

A family of Reynolds number ratios calculated using Eq. (3) is shown in Fig. 3b. It may be noted that the ratios are temperature dependent at flow conditions where Sutherland's viscosity law was applicable. The temperatures ( $T_0$ ) were selected to correspond to the range of total temperatures usually available in wind tunnels.

All of the transition Reynolds numbers presented in this report (including data from other sources) were calculated using Eq. (3) or were obtained from Fig. 3b.

## SECTION IV

### BASIC TRANSITION RESULTS

#### 4.1 METHODS OF DETECTION

A surface pressure probe, microphone, and photography were used to detect transition.

##### 4.1.1 Surface Probe

Typical surface probe transition profiles obtained in Tunnels D and A are presented in Figs. 4 and 5 for several Mach numbers and unit Reynolds numbers. Unless otherwise specified, the location of transition used in this study is defined as the peak in the pitot pressure profile as illustrated in Figs. 4 and 5. This method of transition detection is generally accepted as being near the end of the transition region (Refs. 13 and 14) and has been established as one of the more repeatable and reliable methods of selecting a particular and finite location of transition.

##### 4.1.2 Microphone

Pressure fluctuation profiles obtained with the flush-mounted 1/4-in.-diam surface microphone are shown in Fig. 6. The sharp apex in the pressure profile was defined as the indication of transition at the microphone location. The transition Reynolds number, based on this definition, is compared to the pitot probe values in subsequent figures. It is of interest to note the similarity between the root-mean-square (rms) profiles and other measurements of the transition region, e. g., the surface probe (Figs. 4 and 5), heat-transfer rates (Refs. 15 and 16), and heat-transfer fluctuations (Ref. 17). Additional information on the spectral distribution of the pressure fluctuations in the laminar, transitional, and turbulent boundary layers on this configuration and a description of the microphone instrumentation and recording procedures are reported in Ref. 18.

### 4.1.3 Photographic Observations

The location of transition as determined from schlieren and shadow-graph photographs was selected at the body station where the boundary layer had developed into what appeared visually to be fully turbulent flow. This location of transition provided  $(Re_t)_\delta$  values, in general, about 10 to 20 percent lower than  $(Re_t)_\delta$  results obtained from the surface probe peak pressure locations. Any burst, ripples, or rope effects that were observable upstream of the fully developed turbulent location were ignored in the selection of  $x_t$ . The transition values presented represent an average  $x_t$  value determined from approximately four different photographs.

## 4.2 TRANSITION REYNOLDS NUMBERS

As stated in Section I, one of the primary objectives of this research was to provide sharp cone  $(Re_t)_\delta$  data suitable for direct comparison with existing two-dimensional hollow cylinder data reported in Refs. 8, 9, and 13. To maintain as nearly identical free-stream flow disturbances as possible, the cone was positioned in the tunnel very near the previous hollow cylinder locations and the experiments were conducted at equivalent free-stream Mach number and unit Reynolds number values.

The transition Reynolds number results for Tunnels D and A are presented in Figs. 7 and 8 (see also Tables I and II, Appendix II) and appear quite normal in that they exhibit the usual increase in  $(Re_t)_\delta$  with increasing  $(Re/in.)_\delta$  and the photographic values are about 10 to 20 percent lower than the surface probe values. Although the microphone results were limited to two data points, the peak in the pressure fluctuation profile appears to provide  $(Re_t)_\delta$  values consistent with the surface probe and photographic values.

One of the known (but sometimes forgotten) variables that can affect the transition location is the dew point (temperature at standard atmospheric pressure at which water condensation occurs), Ref. 19. In Tunnel D the dew point was sufficiently low ( $< 0^\circ\text{F}$ ) at all Mach numbers not to affect the  $x_t$  locations. Also, in Tunnel A the dew point was sufficiently low<sup>1</sup> at all Mach numbers except for the lower unit Reynolds numbers (subatmospheric pressure levels) at  $M_\infty = 3$ , as illustrated in Fig. 8a. Therefore,

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<sup>1</sup>The relatively high dew point existing in the  $M_\infty = 3$  data reflects facility limitations existing on that particular date and does not necessarily represent standard test conditions.

a suggested  $(Re_t)_\delta$  trend as indicated by the dashed line has been included in Fig. 8a for  $M_\infty = 3$ .

## SECTION V TRANSITION CORRELATION

The primary objective of this research was to determine if sharp cone transition Reynolds numbers varied with tunnel size in accordance with the previously published planar results and to establish if the  $(Re_t)_\delta$  values could be correlated using the aerodynamic-noise-transition parameters developed by Pate and Schueler, Refs. 8 and 9.

There was a large increase in the cone  $(Re_t)_\delta$  values from Tunnels D and A at all test Mach numbers as can be readily determined by a comparison of the data in Figs. 7 and 8. Figure 9 presents a direct comparison of the  $M_\infty = 4$  cone  $(Re_t)_\delta$  data from Tunnels D and A. The large increase in  $(Re_t)_\delta$  with increasing tunnel size is clearly evident and is very similar to the planar results from Refs. 8 or 9 which are included for a quantitative comparison. The increase in  $(Re_t)_\delta$  with increasing tunnel size is explained by a decrease in the aerodynamic-noise intensities that radiate from the turbulent boundary layer on the tunnel walls. A more comprehensive discussion of this type of disturbance mode and the aerodynamic-noise-transition correlation parameters ( $\delta^*$ ,  $C_F$ , and  $c$ ) is given in Refs. 8 and 9.

Transition Reynolds numbers on sharp slender cones were correlated as shown in Fig. 10 using the aerodynamic-noise-transition parameters developed by Pate and Schueler in Refs. 8 and 9. Data used in the cone correlation were obtained not only from the present investigation, but from a total of ten sources representing ten different wind tunnel facilities. The data covered a free-stream Mach number range from 3 to 14, an  $(Re/in.)_\infty$  range from  $0.1 \times 10^6$  to  $1.2 \times 10^6$ , and test section sizes from 12 in. square to 54 in. in diameter. Specific information on the range of test conditions and pertinent information on model geometry are provided in Table III. Also included in Fig. 10 is the correlation of two-dimensional  $(Re_t)_\delta$  data taken from Refs. 8 and 9. The  $(Re_t)_\delta$  data obtained with detection methods other than a surface probe were adjusted in accordance with the findings of Refs. 13 and 14 as specified in Table III.

One factor that must be recognized in the correlation of cone data is the absence of a one-to-one relation or even a constant ratio between the free-stream and cone surface unit Reynolds numbers. If a series of cone angles had been selected which would have allowed a constant ratio of



certain cone to free-stream parameters - say the unit Reynolds number ratio - to have been maintained, then any relationship that might have existed between the strength of the cone bow shock wave and/or the receptivity of the cone laminar flow to the radiated noise levels after passage through the bow shock would possibly have remained more constant. Future investigations in these areas would, of course, be desirable. Notwithstanding these uncertainties, the cone  $(Re_t)_\delta$  values are shown (Fig. 10) to correlate fairly well without exhibiting a significant dependence on the cone angle. It is perhaps of special interest to note that  $(Re_t)_\delta$  data from the AEDC-VKF Hotshot Tunnel F (Gas Dynamic Wind Tunnel, Hypersonic (F)), although a little low, appear to correlate. In addition to the radiated sound disturbances that are presumed to be present in Tunnel F, there is also the likely possibility that significant free-stream entropy fluctuations (temperature spottiness) are also present. It would be expected that this additional disturbance mode would also have an adverse effect on  $(Re_t)_\delta$ .

An empirical equation for the two-dimensional planar correlation was reported in Refs. 8 and 9 to be

$$\left[ (Re_t)_\delta \right]_{\text{planar}} = \frac{0.0141 (C_F)^{-2.55} \left[ 0.56 + 0.44 \left( \frac{c_1}{c} \right) \right]}{\sqrt{\frac{\delta^*}{c}}} \quad (4)$$

An empirical equation that fits the cone data fairly well can be written as

$$\left[ (Re_t)_\delta \right]_{\text{cone}} = \frac{10.5 (C_F)^{-1.66} \left[ 0.56 + 0.44 \left( \frac{c_1}{c} \right) \right]}{\sqrt{\frac{\delta^*}{c}}} \quad (5)$$

There are several significant results (other than the basic correlation which was independent of Mach number and unit Reynolds number) to be deduced from Fig. 10.

First: The sharp cone and planar correlations appear to intersect at the low  $C_F$  values ( $M_\infty \geq 8$ ) and diverge as  $C_F$  increases ( $M_\infty \rightarrow 3$ ). This trend implies that the ratio of cone to planar  $(Re_t)_\delta$  values is dependent on Mach number, tunnel size, and unit Reynolds number. A detailed discussion on this subject is pursued in Section VII.

Second: A literal interpretation of the correlation suggests that Tunnel F planar  $(Re_t)_\delta$  values would be larger than cone values. The validity of this inference will have to wait for experimental verification.

The average turbulent skin friction coefficients ( $C_F$ ) used in the transition correlation were determined using Ref. 20, in conjunction with the tunnel free-stream Mach number and a length Reynolds number based on  $(Re/in.)_\infty$  and the model axial location ( $\ell_m$ ) as measured from the tunnel throat. Information concerning the determination of the tunnel wall  $\delta^*$  values is provided in Table III.

The reader should be aware that the  $(Re_t)_\delta$  correlations presented in Fig. 10 are applicable only to wind tunnels having turbulent wall boundary layers. Consequently, the correlations cannot be used for evaluation of ballistic range or free-flight transition locations. Furthermore, the experimental data and correlations presented should not be used to reach conclusive decisions regarding the "true" Mach number and unit Reynolds number variations that may exist in a disturbance-free environment (either free-flight or experimental facility). However, it has been established that - at least in conventional supersonic and hypersonic wind tunnels - radiated noise is a major and perhaps dominating influence on the transition location and process.

## SECTION VI

### TUNNEL SIZE AND MACH NUMBER EFFECTS

Significant increases in planar transition Reynolds numbers with increasing tunnel size as a result of a decrease in the radiated aerodynamic noise were thoroughly documented by Pate and Schueler, Refs. 8 and 9. Cone  $(Re_t)_\delta$  data obtained during the present investigation in Tunnels A and D demonstrated a similar increase with increasing tunnel size as was illustrated in Fig. 9.

A composite plot of data from the present study and several other sources is presented in Fig. 11. These results firmly establish the existence of a significant increase in cone and planar  $(Re_t)_\delta$  values with increasing tunnel size. The data presented also clearly indicate that only by comparing data obtained in identical test environments can a valid and meaningful relationship between cone and planar  $(Re_t)_\delta$  ratios be established.

Figure 11 also adds substantial support to the conclusion of Refs. 8 and 9 that the "true" Mach number effect on transition cannot be established from wind tunnel models exposed to aerodynamic noise. It is perhaps also of interest to note the difference in Mach number trends between the cone and planar  $(Re_t)_\delta$  data which exists even when the fairing is based on data from tunnels of similar size.

The predicted  $(Re_t)_\delta$  values obtained using Eqs. (4) and (5) are also included in this figure, and the agreement with the experimental data in both trends and levels is considered quite satisfactory.

Variations of transition with tunnel size are perhaps most strikingly demonstrated at  $M_\infty = 3$  where the cone and planar data are presented for tunnels varying in size from 5 to 40 in. and from 1 to 16 ft, respectively.

Concerning Mach number effects, the reader is referred to the results obtained by Stainback at NASA-Langley (Ref. 21) which were represented and discussed in Refs. 8 and 9. These studies report that when the tunnel and cone local unit Reynolds number were held approximately constant and the cone local Mach number was varied from about 4 to 8 — by proper selection of cone angles — then the  $(Re_t)_\delta$  values were independent of Mach number. These results are in agreement with the proposed aerodynamic-noise-transition relation and with the correlations presented in Fig. 10.

## SECTION VII AXISYMMETRIC AND PLANAR TRANSITION CORRELATION

Potter and Whitfield in Ref. 10 made a qualitative comparison of  $(Re_t)_\delta$  data obtained on cones and planar bodies from several sources and observed that the ratio of  $(Re_t)_\delta, \text{ cone} / (Re_t)_\delta, \text{ planar}$  appeared to decrease from a value of approximately 3 at  $M_\infty \approx 3$  to a value of about 1.1 at  $M_\infty \approx 8$ . Based on the planar results of Pate and Schueler, Refs. 8 and 9, Whitfield and Iannuzzi in Ref. 11 concluded that attempts at comparison of  $(Re_t)_\delta$  from various high-speed facilities as done in Ref. 10 must now be viewed with reservation, and the relationship between cone and planar  $(Re_t)_\delta$  results could not be established from presently available data.

Therefore, one of the primary objectives of this research was to attempt to establish a quantitative correlation of sharp slender cones (axisymmetric) and flat plate-hollow cylinder (planar) transition Reynolds numbers at supersonic and hypersonic speeds.

Based on the results of Refs. 8 and 9, it was realized that a correlation was possible only if cone and flat plate data were obtained in the same test facility, under identical test conditions, using equivalent methods of transition detection. There are no available investigations of the receptivity of a laminar boundary layer to radiated noise. Consequently, it was necessary to obtain  $(Re_t)_\delta$  data exposed to various intensity levels of radiated noise while continuing to maintain a constant free-stream unit

Reynolds number and Mach number if the cone-planar  $(Re_t)_\delta$  relation was to be determined. This was accomplished by obtaining test data in significantly different-sized tunnels (VKF Tunnels A and D).

Presented in Fig. 12 is a correlation of cone and flat plate  $(Re_t)_\delta$  data developed from the data obtained in this study and Refs. 8 and 9 (VKF Tunnels A and D) and data from three other test facilities. Based on the results of Refs. 8 and 9, it can be argued that there are various procedures that are available for reducing this type of data. The three procedures used are outlined in the legend of Fig. 12. The significant conclusions to be drawn from this figure are: (1) The  $(Re_t)_\delta$  ratio appears to be about 2.2 to 2.5 at  $M_\infty = 3$ . (2) The trend decreases monotonically with increasing Mach number to a value of approximately 1.0 to 1.1 at  $M_\infty = 8$ . (3) Close inspection of these results at a given Mach number ( $M_\infty = 3$  to 5) suggests a decrease in the  $(Re_t)_\delta$  ratio with increasing tunnel size. This finding is in agreement with the correlation results presented in Fig. 10. (4) The  $(Re_t)_\delta$  ratio is also slightly dependent on the method of analysis.

An empirical equation for the cone-planar  $(Re_t)_\delta$  ratios can be obtained by ratioing Eqs. (4) and (5).

Then

$$\frac{(Re_t)_\delta, \text{cone}}{(Re_t)_\delta, \text{planar}} = \frac{\text{Eq. (5)}}{\text{Eq. (4)}} = 745 (C_F)^{0.89} \quad (6)$$

Predicted transition ratios using Eq. (6) are presented in Fig. 13 for a large range of tunnel sizes, Mach numbers, and  $(Re/in.)_\infty$  values. The experimental data for the 40- and 50-in. tunnels ( $3 \leq M_\infty \leq 8$ ) are in good agreement with the empirically predicted ratios. The data also indicate, qualitatively at least, a decrease in the transition ratio with an increase in tunnel size.

Many investigators have referenced the analytical analysis of Tetervin, Ref. 12, when attempting to explain the cone-planar  $(Re_t)_\delta$  ratios of approximately three that were observed experimentally. Therefore, it appears of interest to consider Tetervin's theoretical results (Refs. 12, 22, and 23) in some detail.

From Tetervin's theoretical analysis in Ref. 22

$$\frac{(Re_t)_\delta, \text{cone}}{(Re_t)_\delta, \text{planar}} = 1 + 2 \frac{(Re_t)_\delta, \text{planar-minimum}}{(Re_t)_\delta, \text{planar}} \quad (7)$$

The  $(Re_t)_{\delta, \text{planar}}$ -minimum values represent the theoretical minimum transition Reynolds number that can occur on a flat plate, and these values are presented as a function of Mach number and model surface temperature in Ref. 22.

Tetervin's theoretical transition ratio (Eq. (7)) was derived using linear stability theory. As shown by Eq. (7) when  $(Re_t)_{\delta, \text{planar}}$  is near the minimum possible value then the cone-planar ratio approaches a value of three. As  $(Re_t)_{\delta, \text{planar}}$  moves farther downstream then Eq. (7) approaches a value of unity. The assumptions that must be applied to Tetervin's analysis are: (1) free-stream disturbances are nonexistent, or (2) the disturbances affect only the laminar region of instability upstream of the respective  $(Re_t)_{\delta, \text{planar}}$ -minimum locations, or (3) the absorptivity characteristics of the laminar layers on both the cone and flat plate downstream of the  $(x_t)_{\text{planar}}$ -minimum locations are identical. There are no available experimental supersonic data that comply with assumption No. 1, and with disturbances present there is no evidence to support assumptions (2) and (3). Nevertheless, it appears to be of interest to use Eq. (7) and the theoretical  $(Re_t)_{\delta, \text{planar}}$ -minimum values of Ref. 22 in conjunction with the experimental  $(Re_t)_{\delta, \text{planar}}$  values presented in Fig. 11 of this study to estimate a few cone-planar transition ratios. The results are listed in column six of Table IV.

An increased value for Eq. (7) can be obtained if experimentally measured minimum critical Reynolds number (Fig. 3 of Ref. 12, showing the stability data of Schubauer and Skramstad, Laufer and Vrebalovich, and Demetriades) is used instead of the theoretical estimates of Tetervin. Also the  $(Re_t)_{\delta}$  values presented in Fig. 11 (and used in the previous evaluation of Eq. (7)) correspond to the maximum pitot probe pressure location which is on the order of a factor of two downstream of what one might consider as a "measurable" beginning of transition. Incorporating these adjustments into Eq. (7) produces the cone-planar ratios tabulated in column seven of Table IV.

For a factor of three to exist in the estimated cone-planar transition ratio at  $M_{\infty} = 3$  would require, depending on the method of analysis, a two-dimensional  $(Re_t)_{\delta, \text{planar}}$  value of 16,000 to 80,000. To the author's knowledge, these values are on the order of a factor of 10 to 50 below any published data. Therefore, it would seem that the cone to flat plate ratio of three quoted by many investigators as being theoretically predicted by Eq. (7) is perhaps without adequate foundation, and the apparent agreement with experimental data that appeared to exist is perhaps only fortuitous. Similarly, the decrease to approximately one exhibited by the experimental data in Figs. 12 and 13 as the Mach number approaches eight does not appear, based on the results in Table IV, to be explained by

Eq. (7). Based on the available information it is suggested that the absolute values produced by Eq. (7) are, at best, not adequate for accurate predictions or for laying a foundation for analyzing experimental transition results. However, it is of interest to note the trend predicted by Eq. (7) for a constant Mach number when the value of  $(Re_t)_\delta$ , planar-minimum is assumed constant. The cone-planar  $(Re_t)_\delta$  ratio as given by Eq. (7) is seen to decrease with increasing experimental  $(Re_t)_\delta$ -planar values — which will occur with increasing tunnel size or increasing  $(Re/in.)_\infty$  — and this trend is in agreement with the experimental results shown in Figs. 12 and 13.

## SECTION VIII COMPARISON OF TUNNEL AND RANGE RESULTS

Figure 14 presents a direct and quantitative comparison of transition data from sharp slender cones obtained in wind tunnels and an aeroballistic range, Ref. 24, at equivalent local Mach numbers using similar methods of detection. At a comparable  $(Re/in.)_\delta$  value, these data suggest that the range  $(Re_t)_\delta$  data are significantly lower than the tunnel results, even for the 12-in. tunnel.

One major nonsimilarity between the tunnel and range experimental conditions is in the surface temperature ratios. Transition reversals have been predicted theoretically, Ref. 25, and verified experimentally, Refs. 26 and 27, and possible transition reversals have been shown experimentally, Ref. 27. However, to the author's knowledge, there are no experimental data that show transition Reynolds number to decrease below the adiabatic wall value for any degree of surface cooling. Therefore, if comparisons could be made where the model wall to free-stream temperature ratios were comparable, then a larger difference between tunnel and range  $(Re_t)_\delta$  data than suggested by Fig. 14 might exist.

One question that naturally arises is whether adverse environmental or model disturbances could be affecting the range results. Only additional and new experimental range data can answer this question. It is also of interest to note that the data in Fig. 14 indicate a significant difference between the tunnel and range  $Re_t$  versus  $(Re/in.)_\delta$  slope. The significance of the unit Reynolds number effect evident in the range data and the results of preliminary investigations on range noise disturbances have been reported in Ref. 24.

## SECTION IX CONCLUDING REMARKS

The significant results obtained from this experimental research were:

1. Boundary-layer transition measurements made on a sharp, 10-deg total-angle cone in a 12- and 40-in. wind tunnel at Mach numbers from 3 to 4.5 have shown a significant increase in transition Reynolds numbers  $(Re_t)_\delta$  with increasing tunnel size. These variations with tunnel size are in agreement with previously published planar results and provide additional confirmation of the severe adverse effect radiated aerodynamic noise has on transition. The variation of  $(Re_t)_\delta$  with tunnel size is explained by the aerodynamic noise that radiates from the tunnel wall turbulent boundary layer.
2. A correlation of transition Reynolds numbers  $(Re_t)_\delta$  data from ten different wind tunnel facilities covering a Mach number range from 3 to 14, a unit Reynolds number per inch range from  $0.1 \times 10^6$  to  $1.2 \times 10^6$  and tunnel test section sizes from 12 in. square to 54 in. in diameter was developed. The correlation was independent of Mach number and unit Reynolds number and dependent only on the aerodynamic-noise parameters established by Pate and Schueler for planar  $(Re_t)_\delta$  data.
3. These axisymmetric  $(Re_t)_\delta$  data and the resulting aerodynamic-noise-transition correlation provide additional confirmation to the earlier suggestions by Pate and Schueler that extreme caution must be exercised when attempting to establish so-called "true" Mach number and unit Reynolds number trends from transition data obtained in conventional supersonic and hypersonic tunnels because of the strong adverse effect of aerodynamic-noise disturbances.
4. A quantitative correlation of cone to planar transition Reynolds number ratios was developed. The data correlation and an empirical equation (based on the aerodynamic-noise-transition correlation) show a monotonic decrease in the transition ratios with increasing Mach number. A dependence on tunnel size and unit Reynolds number, in addition to the Mach number trend, is also indicated.

5. The theoretical analysis of cone-planar transition ratios developed by Tetervin and often quoted by experimentalists as predicting a factor of three to exist, does not appear to provide a satisfactory explanation of the results presented in this report.
6. Wind tunnel  $(Re_t)_\delta$  results are shown to be significantly higher than ballistic range data at  $M_\delta = 4.3$  and  $(Re/in.)_\delta \approx 0.6 \times 10^6$ . Additional experimental testing is required to explain this apparent anomaly.

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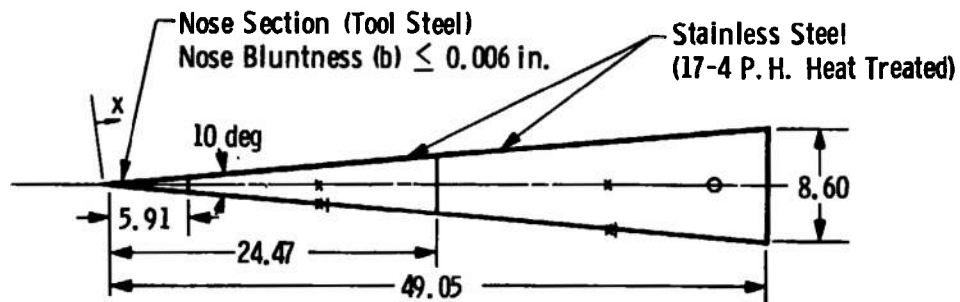
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**APPENDIXES**

**I. ILLUSTRATIONS**

**II. TABLES**



All Dimensions in Inches

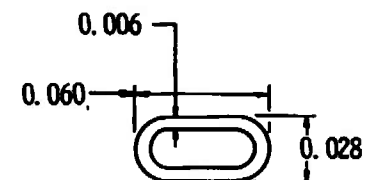
Tunnel D Model Configuration  $\ell = 24.47$  in.

Tunnel A Model Configuration  $\ell = 49.05$  in.

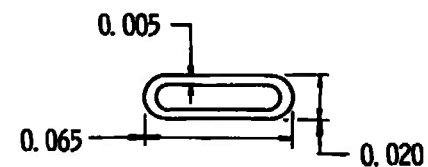
Model Surface Finish 5 to 10 Microinches

Model Instrumentation			
Sym	Type	Quantity	Surface Location x, in.
x	Pressure Orifice, (0.020-in. -diam)	4	15.59, 37.26 (90 deg Apart)
I	Thermocouple	2	16.08, 37.76
o	Microphone	1	45.51

a. Model Details  
Fig. 1 Model Geometry

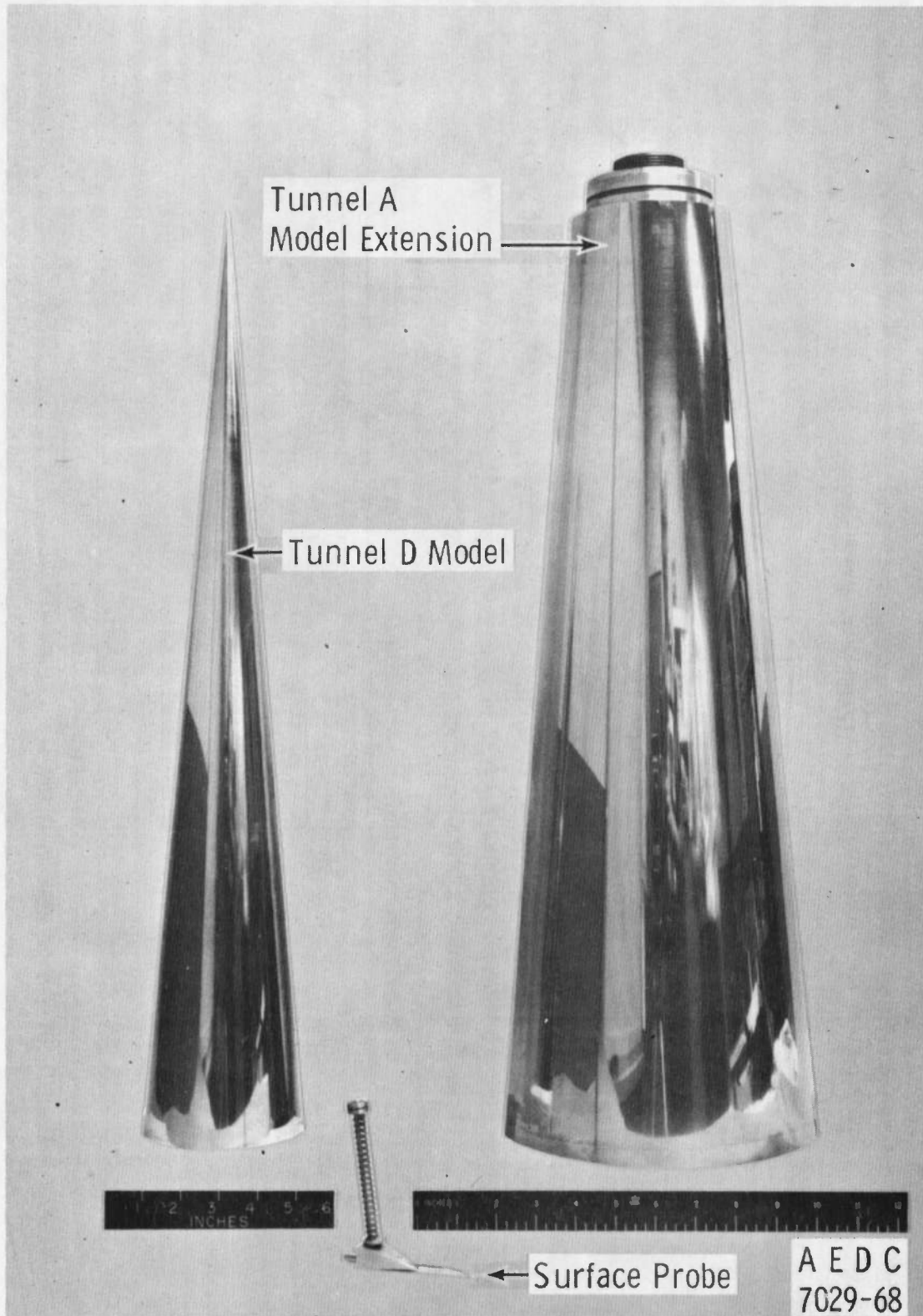


Probe A  
(Used in Tunnels D and A)



Probe B  
(Used in Tunnel A Only)

PROBE DETAILS



b. Photograph of Model Components  
Fig. 1 Concluded

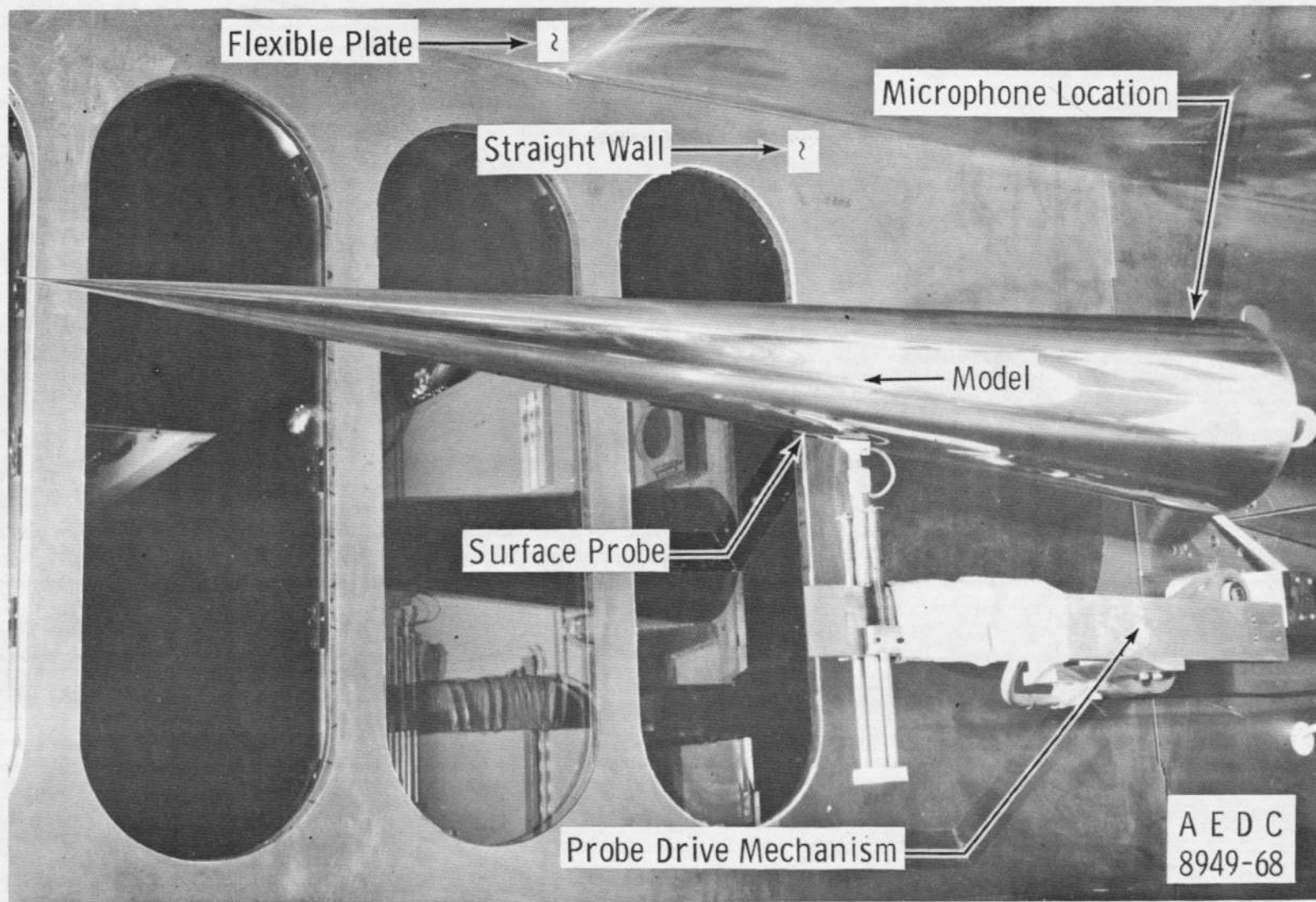
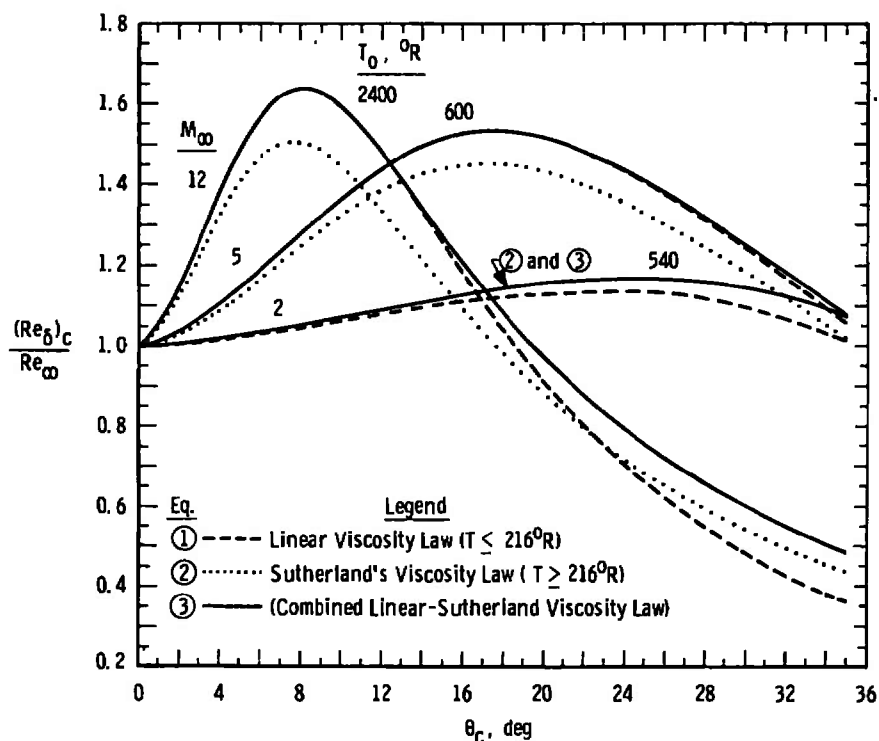
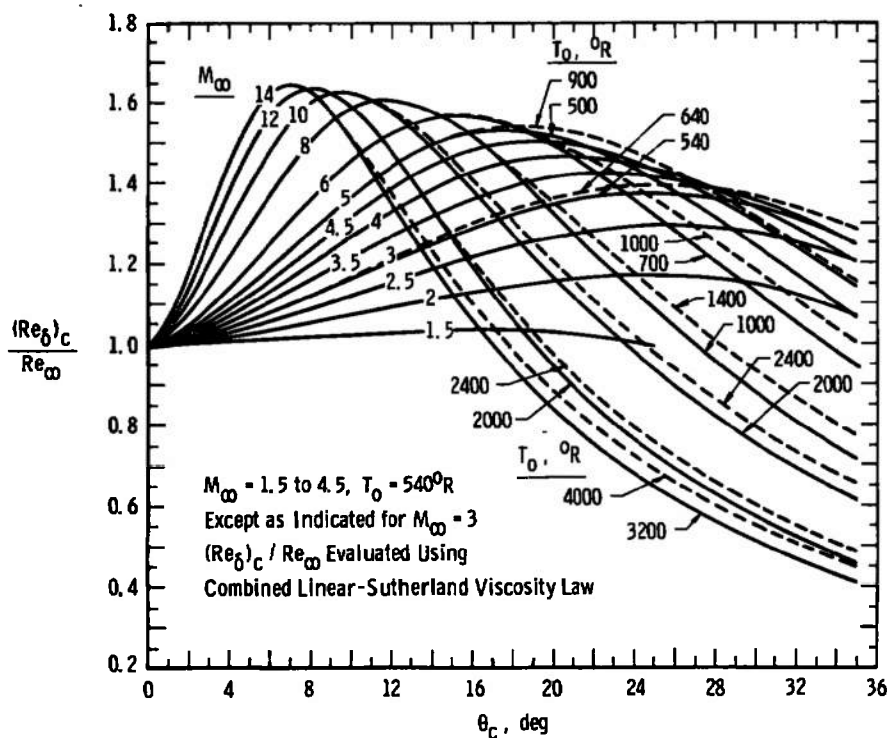


Fig. 2 Tunnel A Cone Model Installation



a. Sensitivity of the Reynolds Number Ratio to Viscosity Determinations

b. Variation of Reynolds Number Ratio with Cone Half-Angle, Mach Number and Temperature  
 Fig. 3 Inviscid Flow, Sharp Cone Reynolds Number Ratios for Air



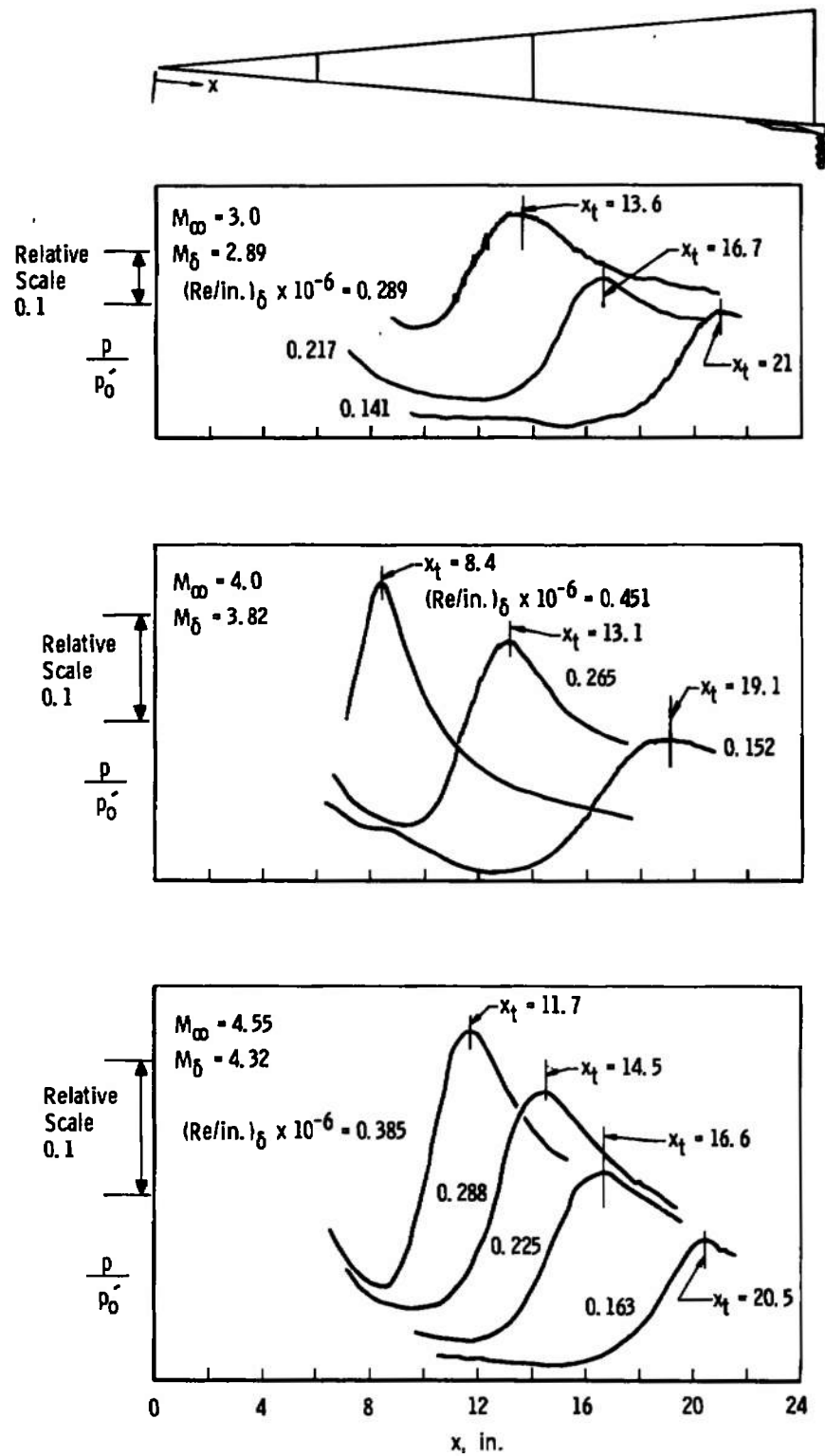


Fig. 4 Examples of Surface Probe Transition Profile Traces (Tunnel D)

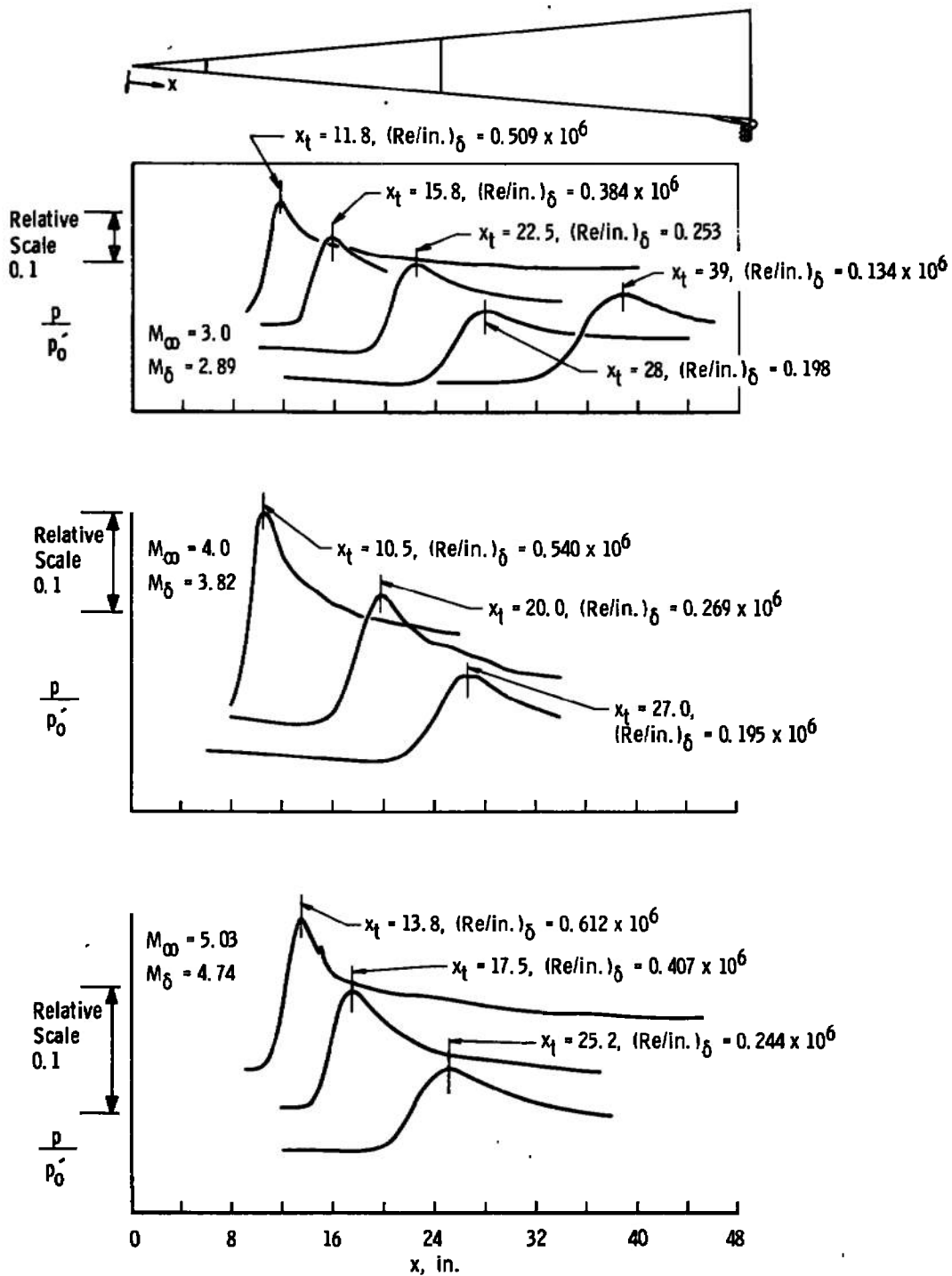


Fig. 5 Examples of Surface Probe Transition Profile Traces (Tunnel A)

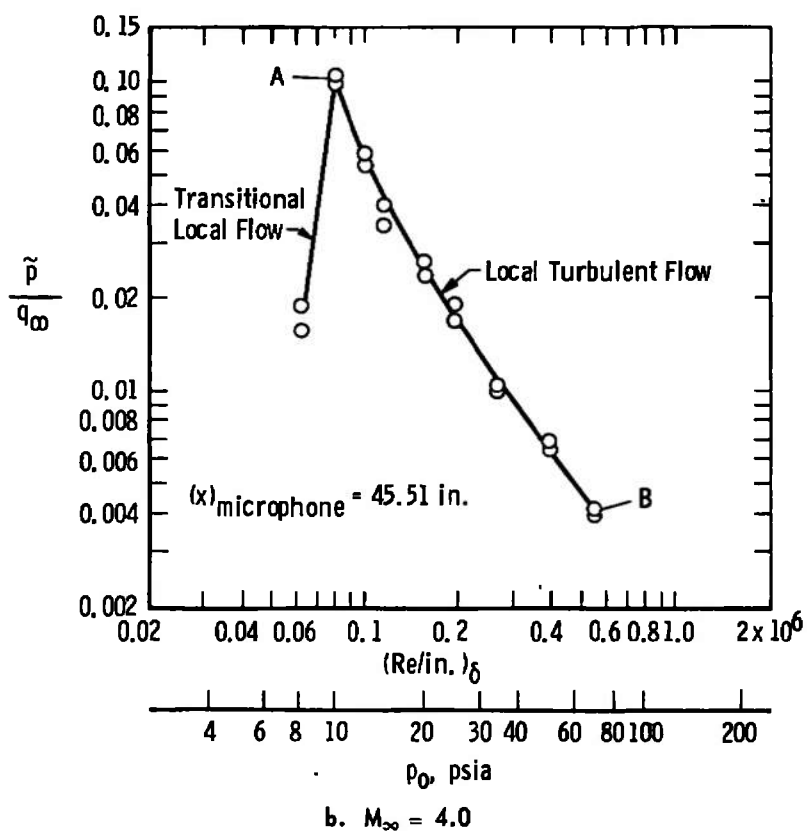
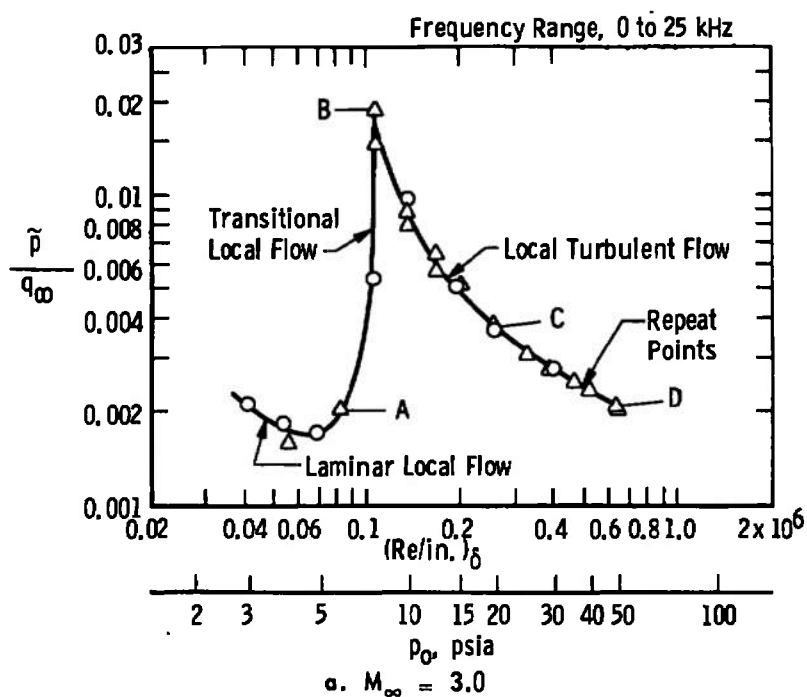


Fig. 6 Indication of Transition from Microphone Root-Mean-Square Pressure Fluctuations,  $M_\infty = 3$  and 4

Sym	Configuration	Surface Ray	Method of Detection	Source	$\ell_m$ , in.
$\triangle$	5-deg Cone	Top	Schlieren	Present Study	44
$\circ$	5-deg Cone	Bottom	Schlieren	Present Study	44
$\square$	5-deg Cone	Bottom	Surface Probe ( $p_{max}$ )	Present Study	44
—	Hollow Cylinder	Bottom	Surface Probe ( $p_{max}$ )	Refs. 8, 9, and 13	48

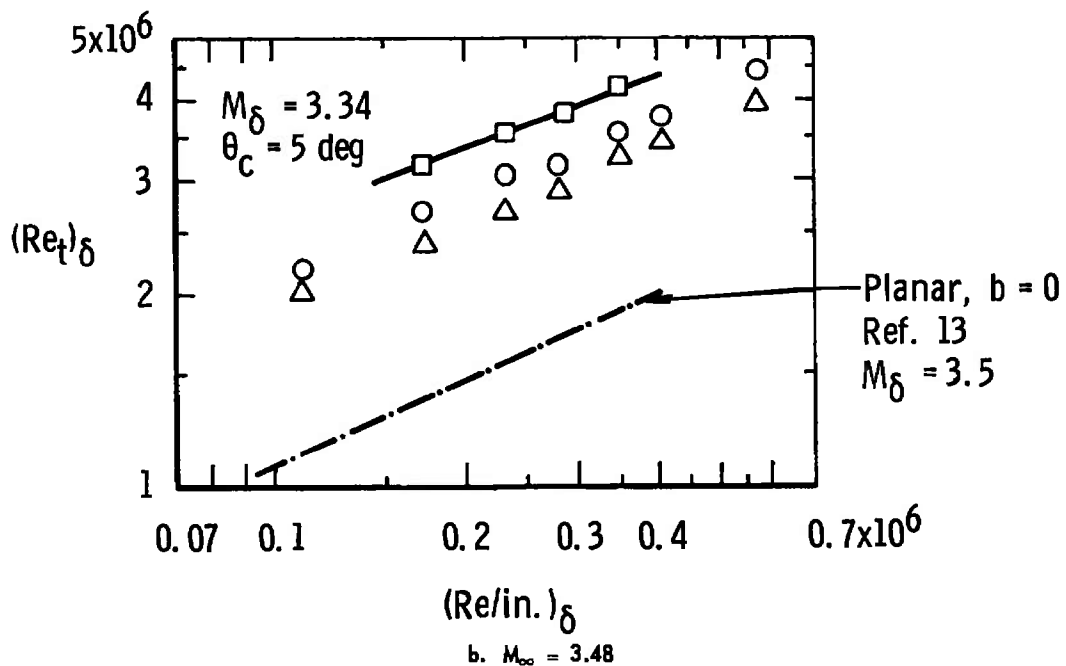
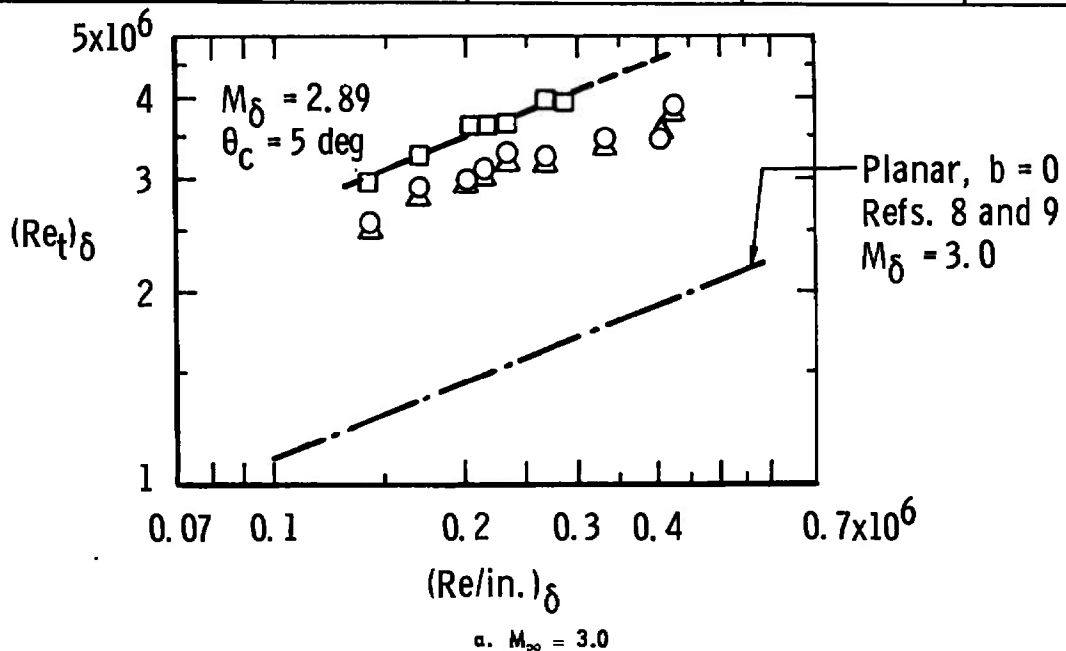
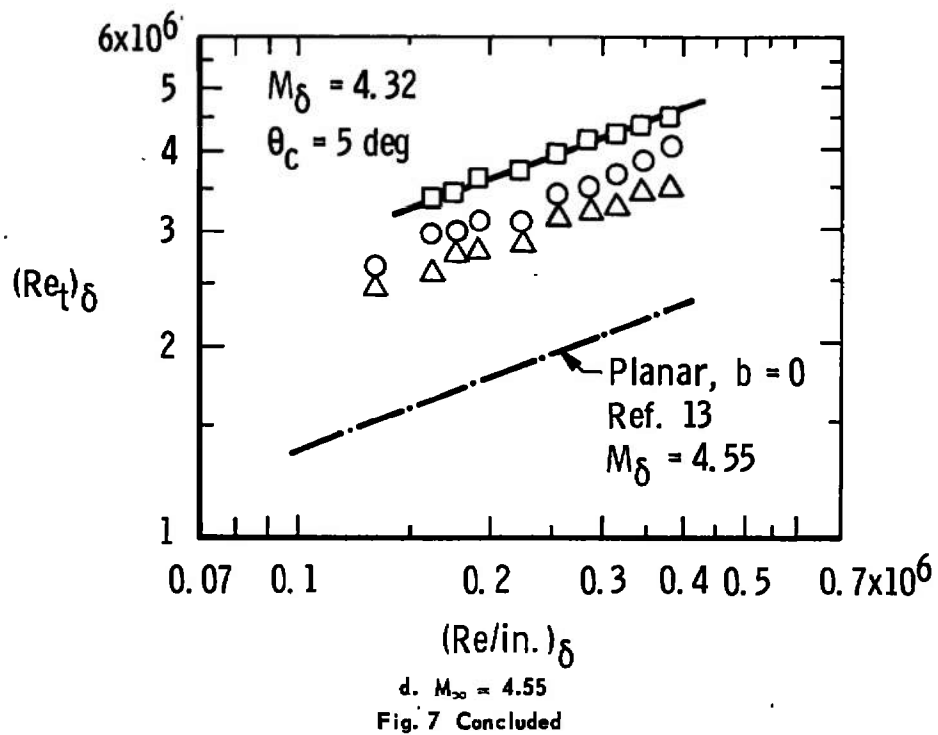
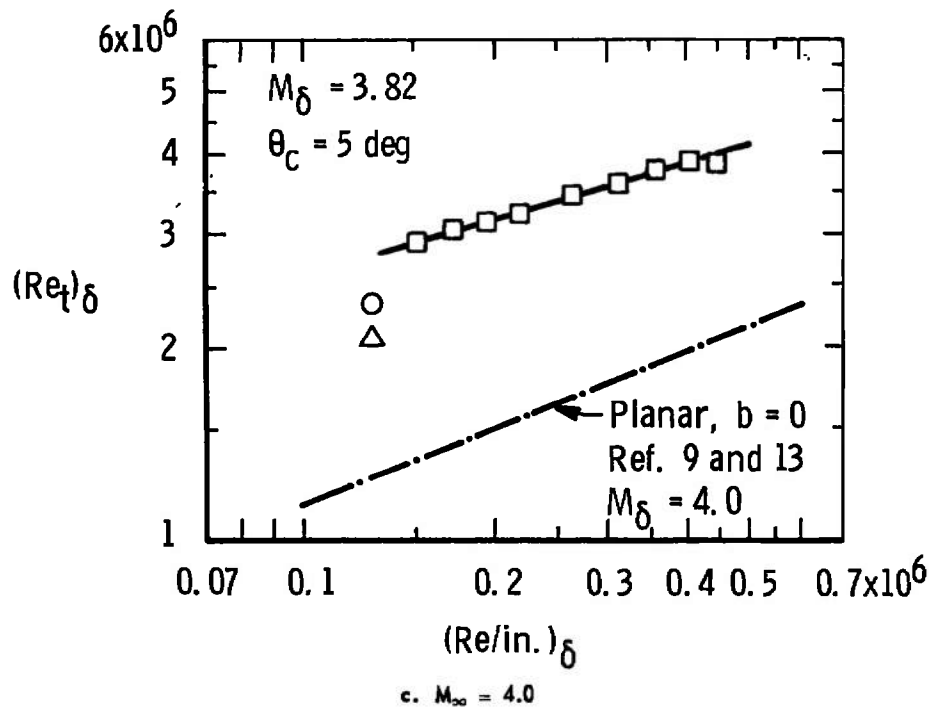


Fig. 7 Transition Reynolds Number Data from Tunnel D, Sharp Cone and Planar Models



Sym	Configuration	Surface Ray	Method of Detection	Source	$l_m$ , in.
$\Delta$	5-deg Cone	Top	Shadowgraph	Present Study	215
$\circ$	5-deg Cone	Bottom	Shadowgraph	Present Study	215
$\square$	5-deg Cone	Bottom	Surface Probe( $p_{max}$ )	Present Study	215
	Hollow Cylinder	Side	Surface Probe( $p_{max}$ )	Refs. 8 and 9	213, 231
$\times$	5-deg Cone	Top	Microphone( $\tilde{p}_{max}$ )	Present Study	215

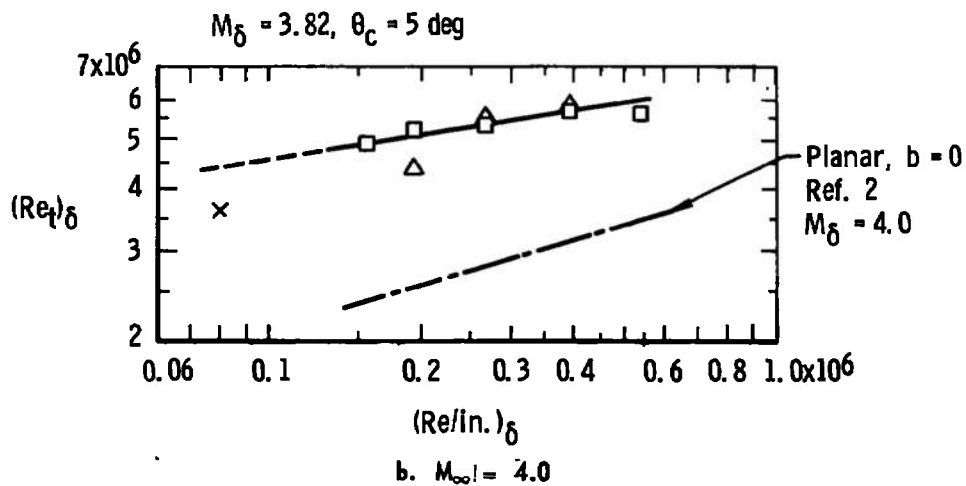
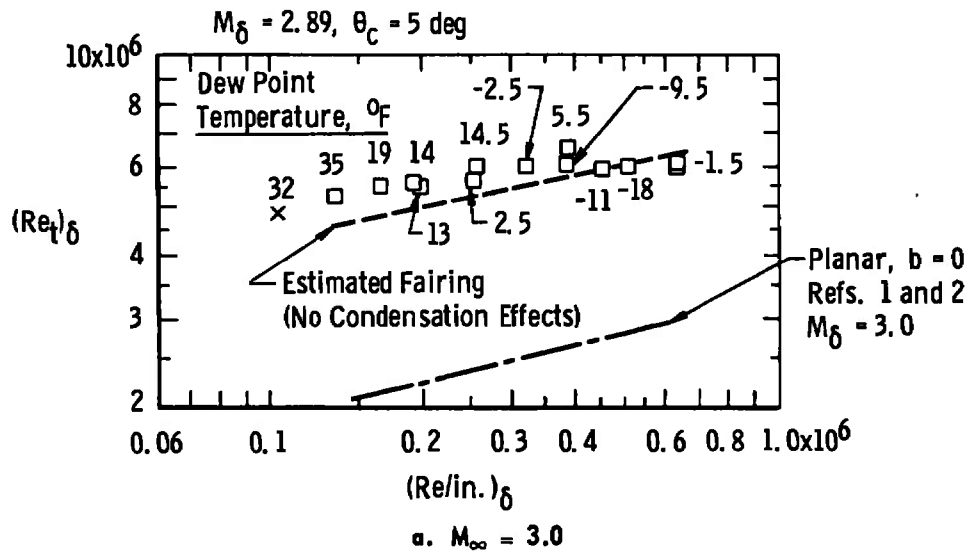


Fig. 8 Transition Reynolds Number Data from Tunnel A, Sharp Cone and Planar Models

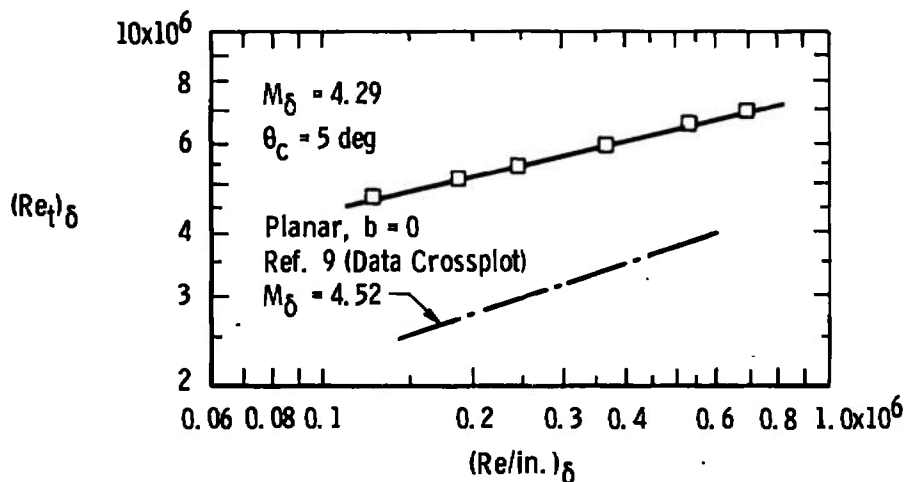
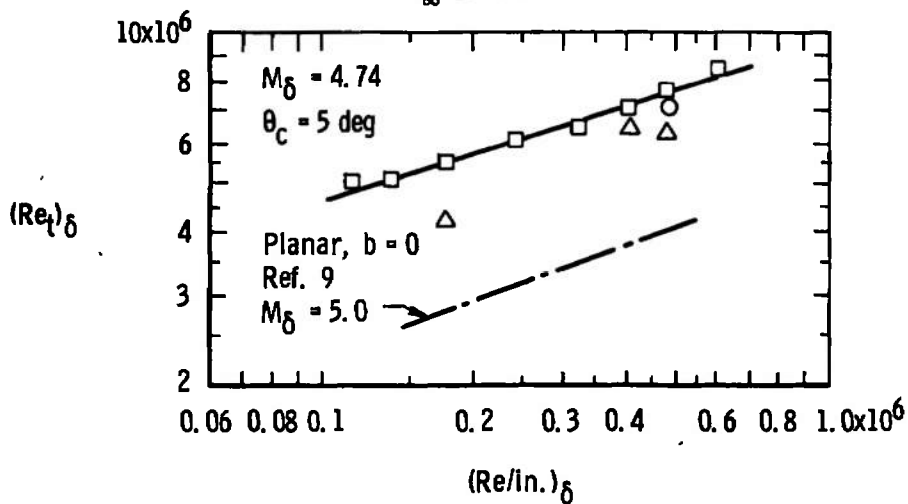
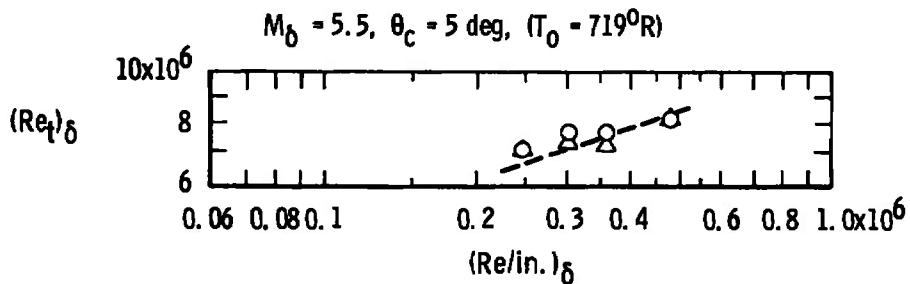
c.  $M_\infty = 4.52$ d.  $M_\infty = 5.03$ e.  $M_\infty = 5.94$ 

Fig. 8 Concluded

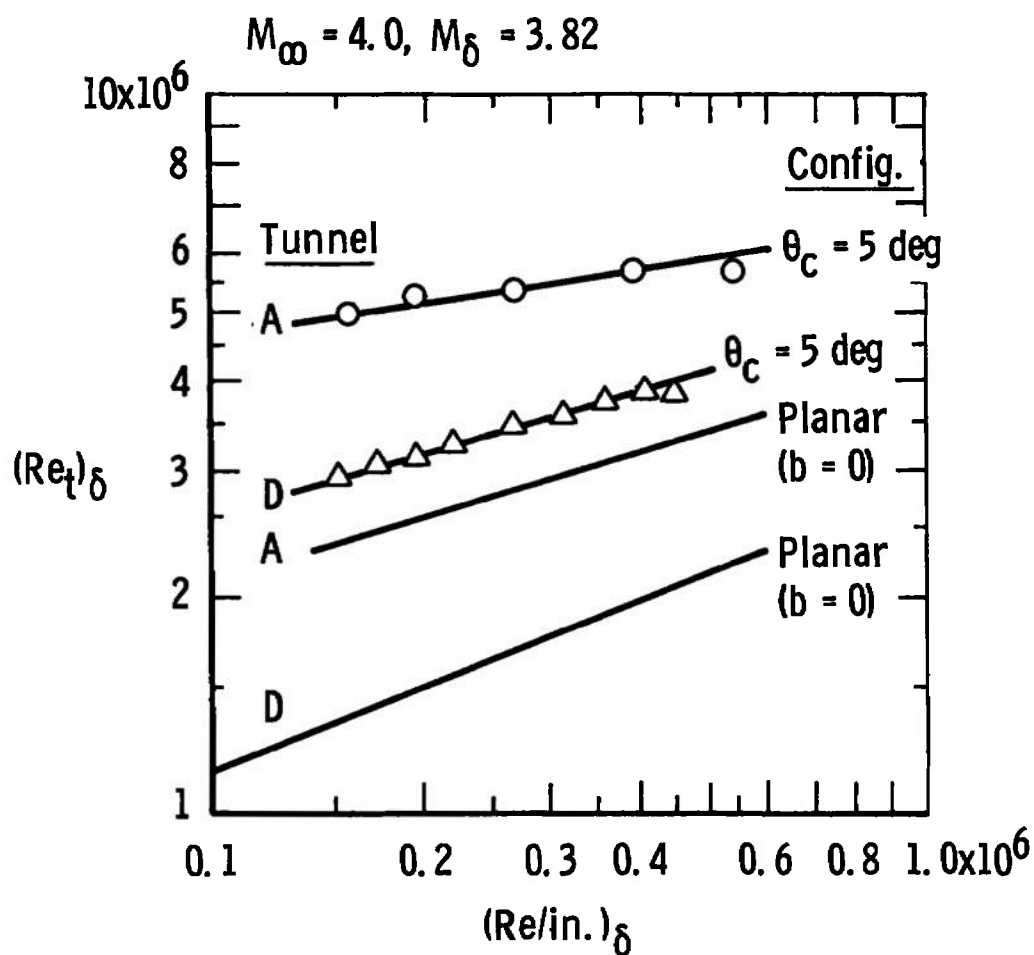


Fig. 9 Variation of Transition Reynolds Numbers with Tunnel Size



Planar Data and Eq. (4) from Refs. 8 and 9. Based on Data from Nine Different Wind Tunnel Facilities Varying in Size from 1 to 16 ft, Mach Number Range from 3 to 8, and  $(Re/in.)_{\infty}$  Range from  $0.05 \times 10^6$  to  $1.1 \times 10^6$ .

Symbol Notation for Cone Data Is Consistent with Table III.

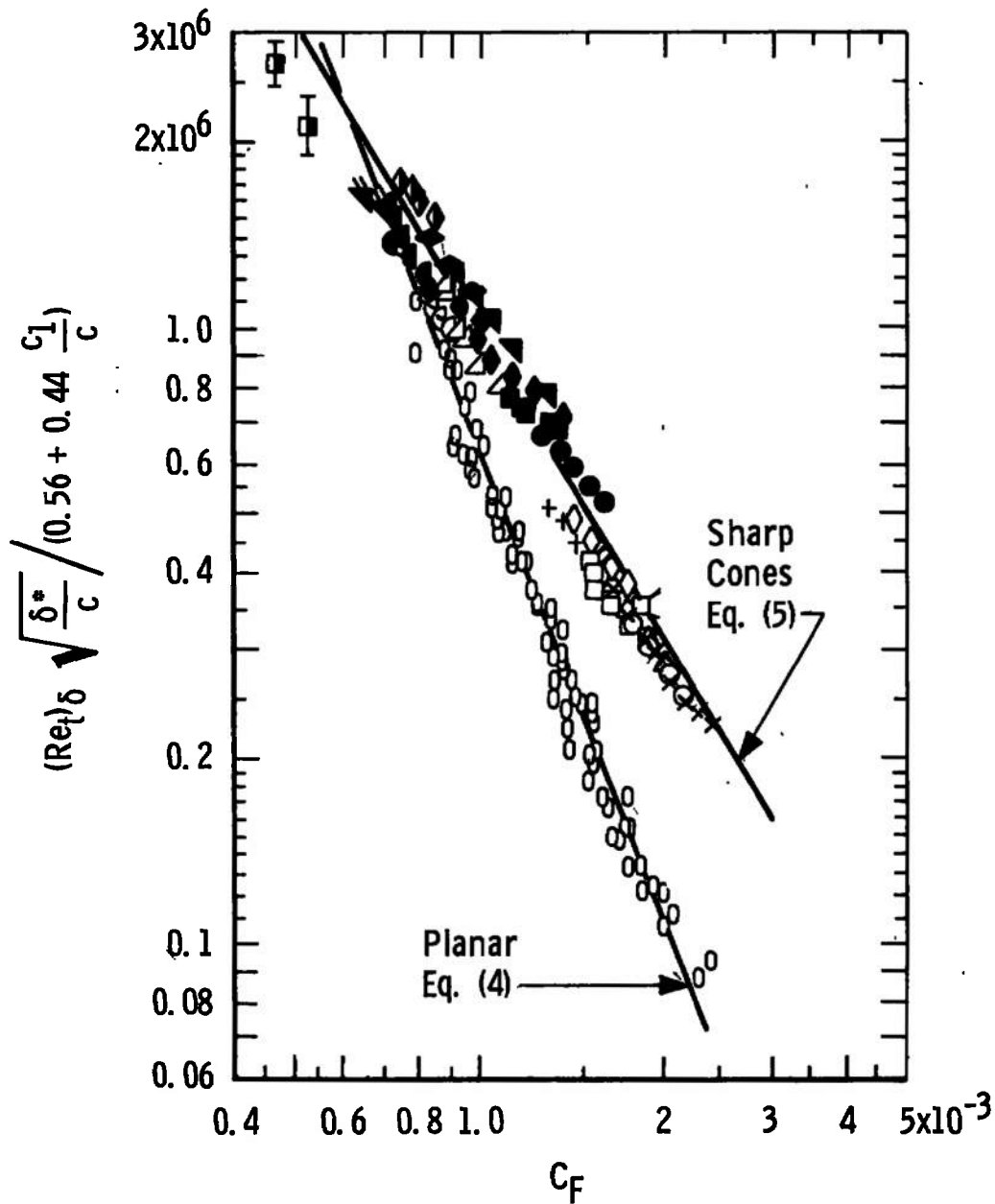


Fig. 10 Correlation of Transition Reynolds Numbers

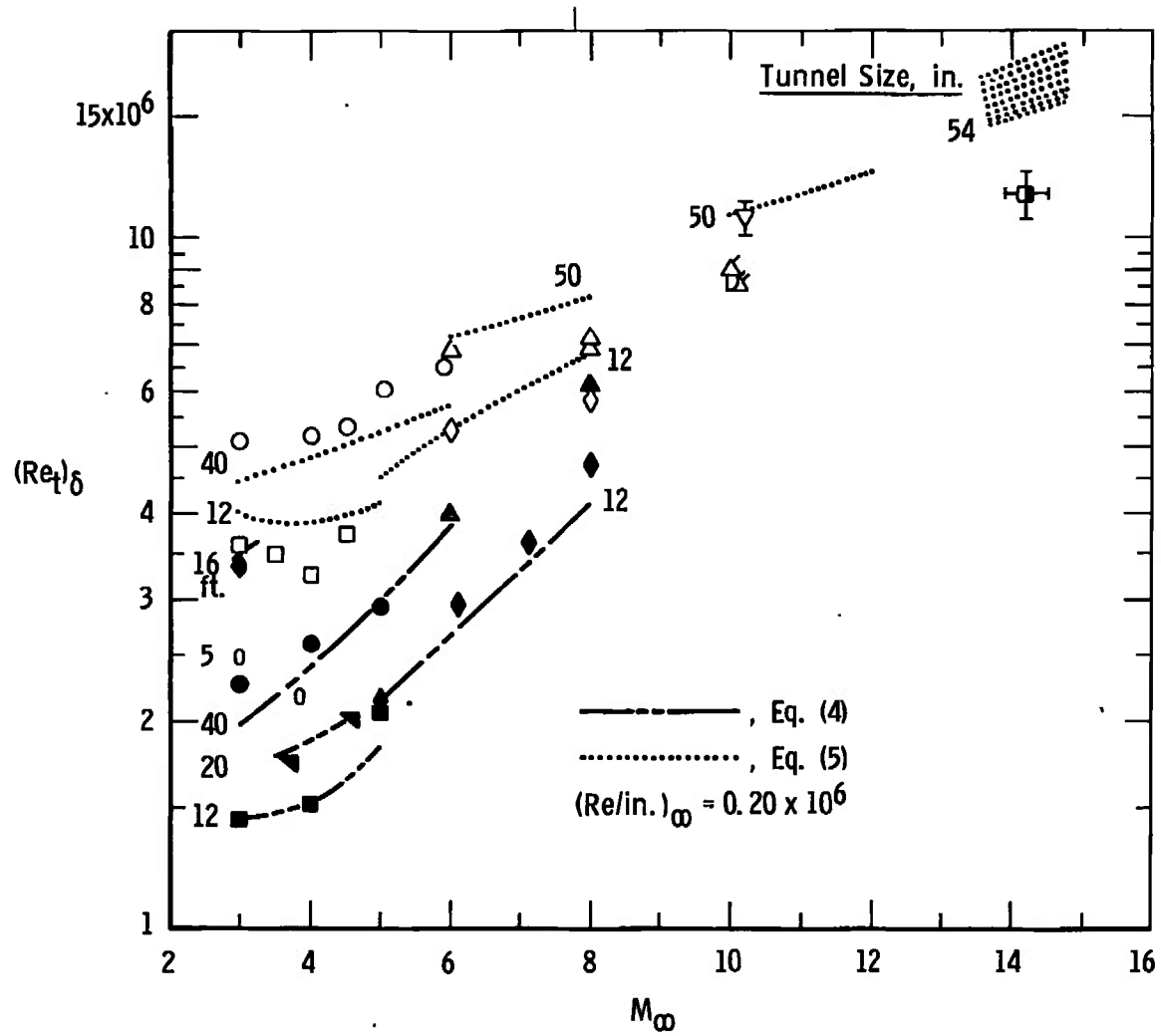


Fig. 11 Variation of Axisymmetric and Planar Transition Reynolds Numbers with Tunnel Size and Mach Number

Sym	$M_\infty$	Configuration	Facility	Source	Method of Detection**
■	3, 4, 5	Hollow Cylinder, $b = 0$	AEDC VKF D(12 by 12 in.)	Refs. 8 and 9	Maximum P (No Adjustment)**
◆	5, 6, 1, 7, 1, 8	Flat Plate, $b = 0$	AEDC-VKF-E(12 by 12 in.)	Refs. 8 and 9	Maximum P (No Adjustment)**
▼	3, 7, 4, 6	Flat Plate, $b = 0$	JPL-SWT (18 by 20 in.)	Refs. 8 and 9	Maximum Surface Shear (No Adjustment)**
●	3, 4, 5	Hollow Cylinder, $b = 0$	AEDC-VKF-A (40 by 40 in.)	Refs. 8 and 9	Maximum P (No Adjustment)**
▲	6, 8	Hollow Cylinder and Flat Plate, $b = 0$	AEDC-VKF-B (50-in. Diam)	Refs. 8 and 9	Maximum P (No Adjustment)**
•	3	Hollow Cylinder	AEDC-PWT-16S (16 by 16 ft)	Refs. 8 and 9	Maximum P (No Adjustment)**
□	3, 3.5, 4, 4.5	Sharp Cone, $\theta_c = 5$ deg	AEDC VKF-D (12 by 12 in.)	Present Study	Maximum P (No Adjustment)**
○	3, 4, 4.5, 5, 5.9	Sharp Cone, $\theta_c = 5$ deg	AEDC-VKF-A (40 by 40 in.)	Present Study	Maximum P ( $M_\infty = 5.9$ , Shadowgraph) (No Adjustment)**
◊	6, 1, 8	Sharp Cone, $\theta_c = 10$ deg	AEDC-VKF-E (12 by 12 in.)	Ret. 10	Shadowgraph (Adjusted by Factor of 1.1)
◊	3, 1, 3.8	Sharp Cone, $\theta_c = 7.5$ deg	R. A. E. (5 by 5 in.)	Ret. 36	Shadowgraph (No Adjustment)
√	10, 2	Sharp Cone, $\theta_c = 3.75$ deg	NASA Langley (31 by 31 in.)	Ref. 34	Maximum $q$ ( $0.4 < (T_w/T_0) < 0.63$ ) (No Adjustment)
D	10	Sharp Cone, $\theta_c = 5$ deg	Republic Aviation Corp. (36-in. Diam)	Ref. 37	Maximum $q$ ( $0.075 < (T_w/T_0) < 0.36$ ) (No Adjustment)
Λ	10	Sharp Cone, $\theta_c = 6$ deg	AEDC-VKF-C (50-in. Diam)	Ref. 33	Maximum $q$ ( $(T_w/T_0) = 0.25$ ) (No Adjustment)
Δ	8	Sharp Cone, $\theta_c = 9$ deg	AEDC-VKF-B (50-in. Diam)	VKF and Ref. 10	Shadowgraph ( $(T_w/T_0) \approx 0.8$ , Hot Wall) (No Adjustment)
Δ	6	Sharp Cone, $\theta_c = 6$ deg	AEDC-VKF-B (50-in. Diam)	VKF and Ref. 10	Maximum $q$ ( $(T_w/T_0) \approx 0.63$ ) (Adjusted by Factor of 1.08)
Λ	10	Sharp Cone, $\theta_c = 9$ deg	AEDC-VKF-C (50-in. Diam)	VKF	Shadowgraph ( $(T_w/T_0) \approx 0.66$ , Hot Wall) (Adjusted by Factor of 1.1)
■	14.2 ± 0.3	Sharp Cone, $\theta_c = 9$ deg	AEDC-VKF-F (54-in. Diam)	Ref. 11	Maximum $q$ ( $(T_w/T_0) \approx 0.19$ ) (No Adjustment)

\*Extrapolated Data

\*\*Amount of Adjustment Based on Results of Present Study and Refs. 10, 13, and 14

Fig. 11 Concluded

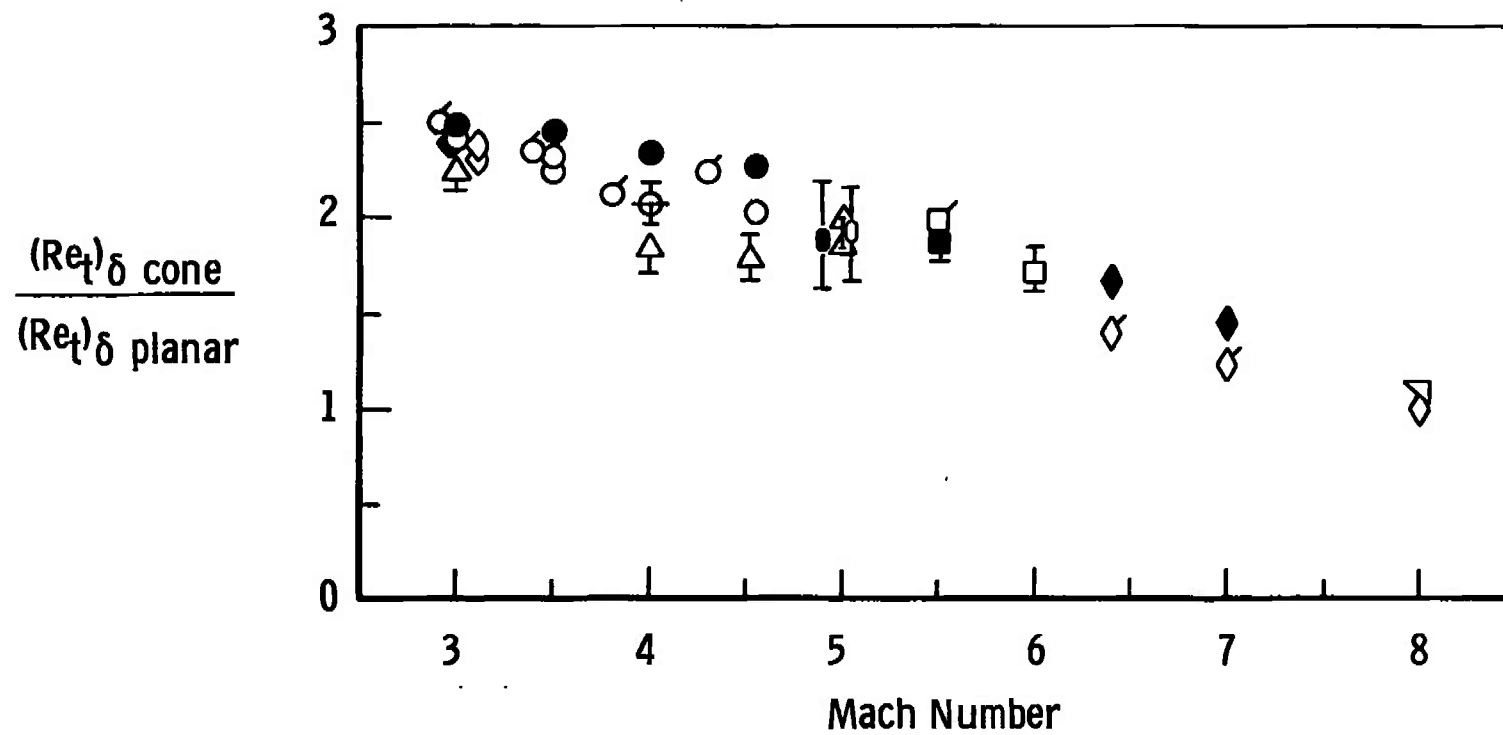


Fig. 12 Correlation of Axisymmetric and Planar Transition Reynolds Number Ratios

Sym	Configuration	$\theta_c$ , deg	$M_\infty$	$M_\delta$	$(Re/in.)_\delta \times 10^{-6}$ Range	Facility	Method-of-Detection	Source
○	Sharp Cone	5	3 to 4.5	2.9 to 4.3	0.15 to 0.4 ↓	VKF-D (12 by 12 in.) ↓	Maximum Pitot Pressure ↓	Present Study (Fig. 7)
	Hollow Cylinder (b = 0)	-	3 to 4.5	3 to 4.5				Refs. 8, 9, and 13
△	Sharp Cone	5	3 to 5	2.9 to 4.7	0.15 to 0.6 ↓	VKF-A (40 by 40 in.) ↓	Maximum Pitot Pressure ↓	Present Study (Fig. 8)
	Hollow Cylinder (b = 0)	-	3 to 5	3 to 5				Ref. 9
□	Sharp Cone	5, 6	6	5.5	0.15 to 0.4 ↓	VKF-A and VKF-B (50-in. Diam)	Shadowgraph $\dot{q}_{\text{maximum}}$	Present Study VKF
	Flat Plate (b ≈ 0)	-	6	6				Refs. 9 and 38
◇	Sharp Cone	6, 9	8	7.0, 6.4	0.2, 0.3 ↓	VKF-B (50-in. Diam)	$\dot{q}_{\text{max}}$ and Shadowgraph	Refs. 10 and VKF
	Hollow Cylinder (b = 0)	-	8	8			$ITw_{\text{max}}$ and Pitot Pressure	Ref. 14
▽	Sharp Cone	6, 9	8	7.0, 6.4	0.2 ↓	VKF-B (50-in. Diam)	$\dot{q}_{\text{max}}$ and Shadowgraph	Ref. 10 and VKF
	Flat Plate (b ≈ 0)	-	8	8			Pitot Pressure	Ref. 39
◊	Sharp Cone	5	3.1	2.98	0.1 to 0.6	NACA-Lewis (12 by 12 in.)	$T_w \text{ max}$	Ref. 15
	Hollow Cylinder	-	3.1	3.1				
◦	Sharp Cone	2.5	5.0	4.90	0.15 to 0.5	NASA-Lewis (12 by 12 in.)	$T_w \text{ max}$	Ref. 16
	Hollow Cylinder	-	5.0	5.0				

Flagged Symbols - Evaluated at Equivalent  $(Re/in.)_\delta$  and  $M_\delta$  Values ( $(Re/in.)_\delta = 0.2 \times 10^6$ )

Open Symbols - Evaluated at Equivalent  $(Re/in.)_\delta$  and  $M_\infty$  Values

Solid Symbols - Evaluated at Equivalent  $(Re/in.)_\infty$  and  $M_\delta$  Values (From Data Cross Plots)

Fig. 12 Concluded

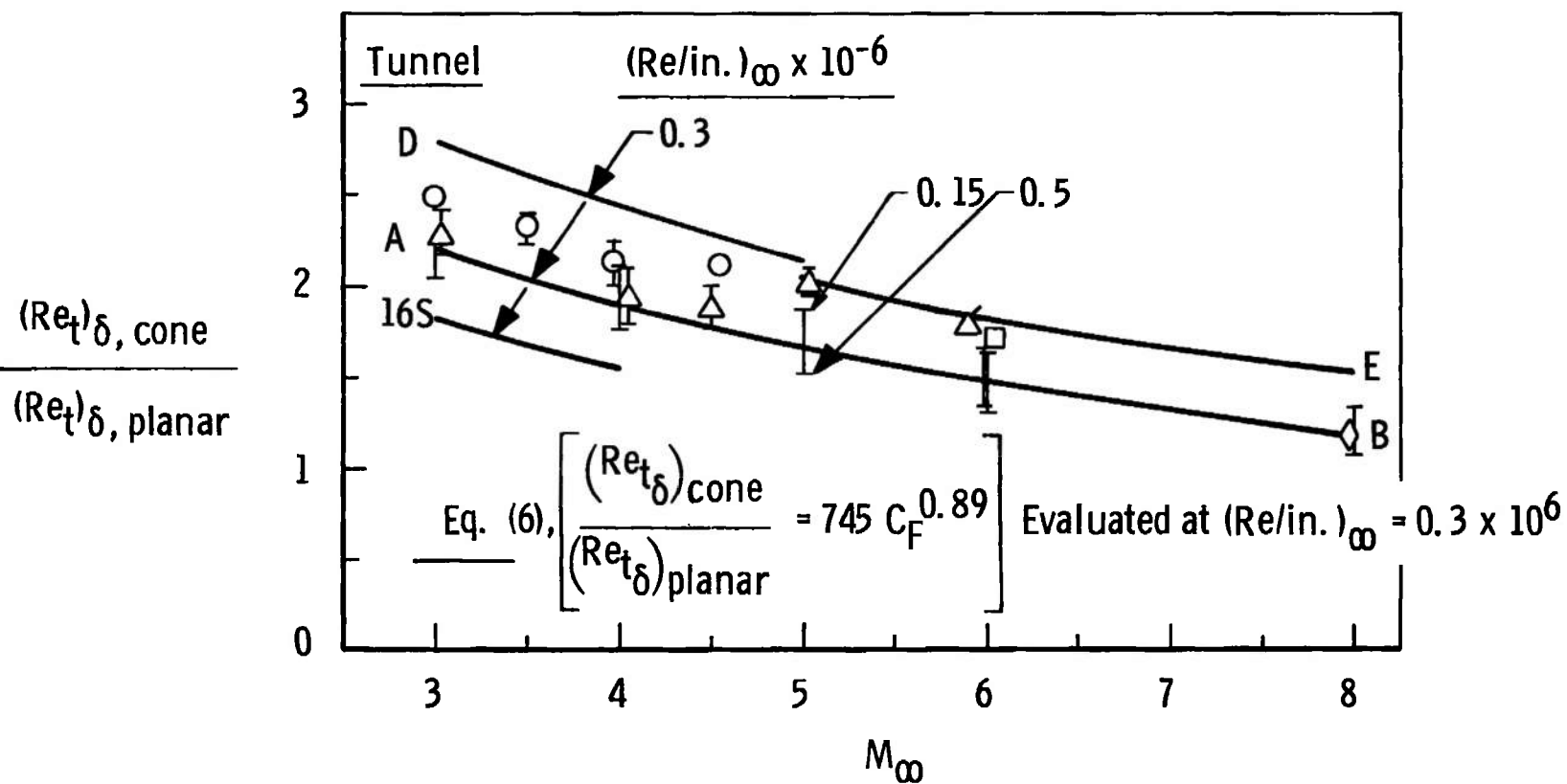


Fig. 13 Comparison of Predicted and Measured Cone-Planar Transition Ratios

Experimental Data Evaluated at Equivalent  $(Re/in.)_{\infty}$  and  $M_{\infty}$  Values

Sym	Configuration	$\theta_c$ , deg	$M_{\infty}$	$M_{\delta}$	$(Re/in.)_{\infty} \times 10^{-6}$ Range	Facility	Method of $x_t$ Detection	Source
○	Sharp Cone	5	3 to 4.5	2.9 to 4.3	0.15 to 0.5	VKF-D (12 by 12 in.)	Maximum Surface Pitot Probe Pressure	Present Study
	Hollow Cylinder (b = 0)	-	3 to 4.5	3 to 4.5	0.15 to 0.5			Refs. 9 and 13
△	Sharp Cone	5	3 to 5	2.9 to 4.7	0.15 to 0.5	VKF-A (40 by 40 in.)	Maximum Surface Pitot Probe Pressure	Present Study
	Hollow Cylinder (b = 0)	-	3 to 5	3 to 5	0.15 to 0.5			Ref. 9
△	Sharp Cone	5	5.9	5.5	0.2	VKF-A (40 by 40 in.)	Schlieren Schlieren	Present Study
	Hollow Cylinder (b = 0)	-	5.9	5.9	0.2			Data Extrapolation from Refs. 8 and 9
□	Sharp Cone	6	6	5.5	0.2	VKF-B (50-in. Diam)	Adjusted Max Heat Transfer (Adjusted by 1.08)	Ref. 10 and VKF
	Flat Plate (b = 0)	-	6	6	0.2		Maximum Pitot Press.	Refs. 9 and 38
◇	Sharp Cone	6, 9	8	7.0, 6.4	0.15 to 0.3	VKF-B (50-in. Diam)	Maximum Heat Trans. (No Adjustment)	Ref. 10 and VKF
	Hollow Cylinder (b = 0)	-	8	8	0.15 to 0.3		Maximum Pitot Press.	Ref. 14

Fig. 13 Concluded

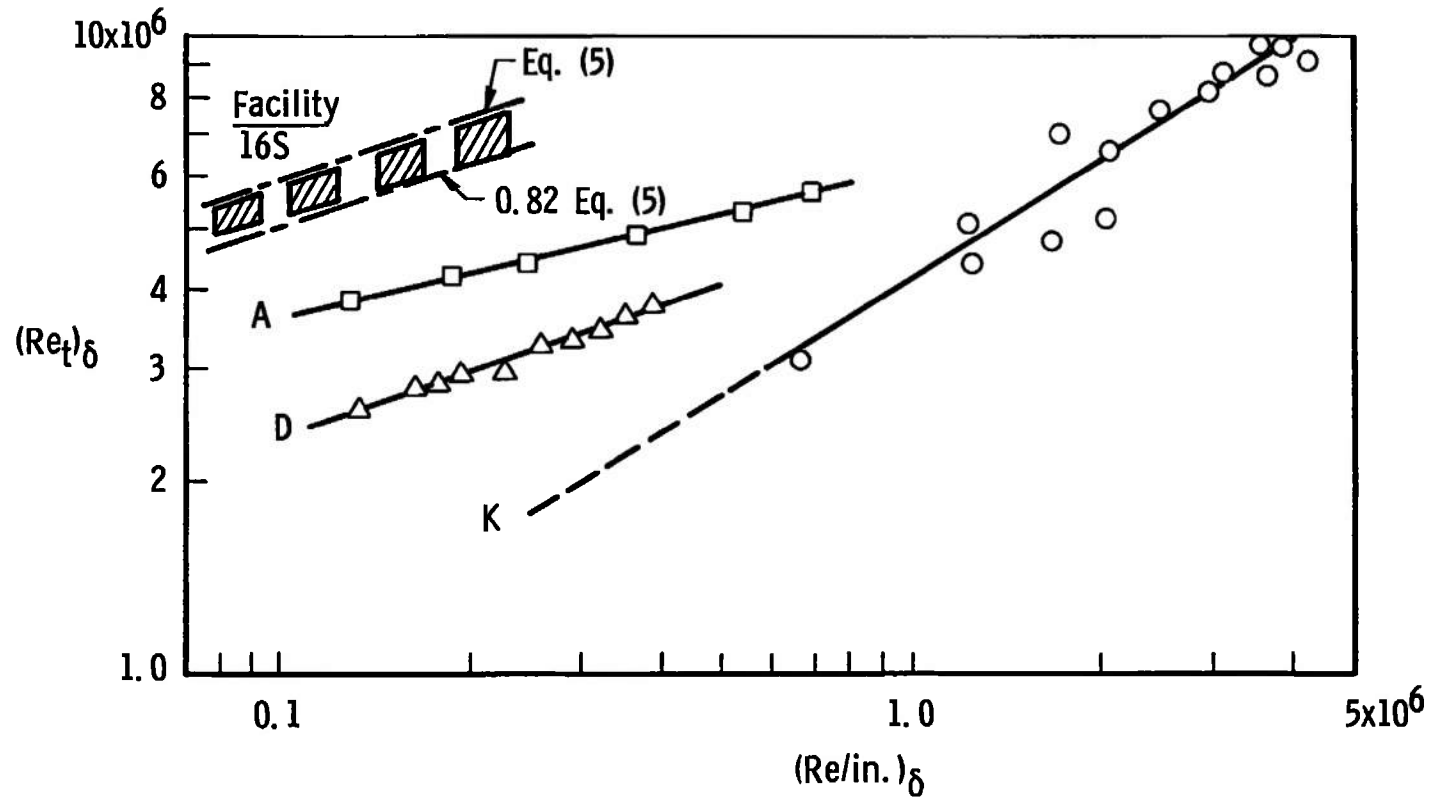


Fig. 14 Comparison of Sharp Cone Transition Reynolds Numbers from Wind Tunnels and an Aeroballistic Range



<u>Sym</u>	<u>Facility</u>	<u><math>M_\delta</math></u>	<u><math>T_w/T_{aw}</math></u>	<u><math>\theta_c</math>, deg</u>	<u>Source</u>	<u>Method of Detection</u>
○	VKF Range K	4.3	$\approx 0.18$	10	Ref. 24	Shadowgraph - Schlieren
△	VKF Tunnel D (12 by 12 in.)	4.3	$\approx 1.0$	5	Present Study	Schlieren
□	VKF Tunnel A (40 by 40 in.)	4.3	$\approx 1.0$	5	Present Study	Surface Pitot Probe Maximum Value Adjusted to Schlieren Location $(Re_t)_{schlieren} \approx 0.82 (Re_t)_{p_{max}}$
▨	PWT-Tunnel 16S (16 by 16 ft)	4.3	$\approx 1.0$	5	Present Study and Refs. 8 and 9	Estimated from Two-Dimensional Data Surface Probe Data

Fig. 14 Concluded

**TABLE I**  
**TUNNEL D TRANSITION REYNOLDS NUMBER, 10-DEG TOTAL-ANGLE SHARP CONE**

$M_\infty$	$M_C = M_\delta$	$p_O$ , psia	$T_O$ , °R	$(Re/in.)_\infty \times 10^{-6}$	$(Re/in.)_\delta \times 10^{-6}$	$x_t$ , * in.	$(Re_t)_\delta \times 10^{-6}$
2.98	2.87	9.93	533	0.133	0.141	≈21	≈2.97
2.99	2.88	14.9	524	0.204	0.217	16.7	3.62
3.00	2.89	20.0	523	0.272	0.289	13.6	3.93
2.98	2.87	9.86	532	0.133	0.141	≈21	≈2.96
2.99	2.88	12.4	544	0.160	0.170	19.3	3.28
2.99	2.88	14.9	548	0.191	0.203	17.8	3.61
3.00	2.89	17.4	549	0.220	0.234	15.7	3.67
3.00	2.89	20.0	549	0.253	0.269	14.8	3.98
3.48	3.34	15.0	520	0.160	0.172	18.5	3.18
3.48	3.34	20.0	516	0.215	0.232	15.3	3.54
3.48	3.34	24.8	514	0.269	0.289	13.2	3.82
3.48	3.34	30.0	513	0.326	0.350	12.0	4.20
3.99	3.81	17.5	530	0.139	0.152	19.1	2.91
4.00	3.82	20.0	528	0.159	0.174	17.6	3.07
4.00	3.82	22.5	526	0.180	0.197	15.8	3.12
4.00	3.82	24.9	523	0.201	0.220	14.7	3.24
4.00	3.82	29.9	521	0.242	0.265	13.1	3.47
4.00	3.82	34.9	518	0.286	0.313	11.5	3.60
3.99	3.81	39.9	518	0.328	0.359	10.5	3.77
3.99	3.81	45.0	517	0.371	0.407	9.4	3.83
3.99	3.81	50.0	518	0.411	0.451	8.4	3.78
4.55	4.32	24.9	539	0.146	0.163	≈20.5	3.34
4.56	4.33	27.4	540	0.159	0.177	19.5	3.46
4.56	4.33	29.9	542	0.173	0.193	18.9	3.65
4.56	4.33	34.9	543	0.202	0.225	16.6	3.74
4.56	4.33	39.9	544	0.229	0.255	15.6	3.98
4.56	4.33	45.0	546	0.258	0.288	14.5	4.17
4.56	4.33	49.9	547	0.285	0.318	13.5	4.29
4.56	4.33	55.0	548	0.312	0.348	12.6	4.38
4.55	4.32	60.0	546	0.345	0.385	11.7	4.50

\* $x_t$  Determined from Surface Probe Peak Pressure

**TABLE II**  
**TUNNEL A TRANSITION REYNOLDS NUMBERS, 10-DEG TOTAL-ANGLE SHARP CONE**

$M_\infty$	$M_C = M_\delta$	$P_{O_2}$ , psia	$T_{O_2}$ , °R	$(Re/in.)_\infty \times 10^{-6}$	$(Re/in.)_\delta \times 10^{-6}$	$x_t$ , * in.	$(Re_t)_\delta \times 10^{-6}$	Dew Point Temperature, °F
2.99	2.88	19.8	562	0.243	0.258	23.3	6.01	14.5
2.99	2.88	29.7	562	0.364	0.387	17.0	6.57	5.5
2.99	2.88	14.8	565	0.181	0.192	29.0	5.57	14.0
2.98	2.88	10.1	561	0.126	0.134	39.2	5.25	35
3.00	2.89	49.9	566	0.603	0.640	9.5	6.08	- 1.5
3.00	2.89	49.6	569	0.596	0.633	9.3	5.89	- 1
3.00	2.89	39.8	568	0.479	0.509	11.8	6.00	-18
3.00	2.89	35.0	566	0.424	0.450	13.3	5.99	-11
2.99	2.88	29.6	565	0.362	0.384	15.8	6.07	- 9.5
2.99	2.88	24.7	563	0.303	0.322	18.7	6.02	- 2.5
2.99	2.88	19.7	568	0.238	0.253	22.5	5.69	2.5
2.99	2.88	15.1	562	0.186	0.198	28.0	5.53	13
2.98	2.87	12.6	561	0.156	0.166	33.2	5.51	19
4.02	3.84	69.9	569	0.493	0.540	10.5	5.67	-10.5
4.02	3.84	50.0	562	0.359	0.394	14.6	5.75	-10
4.02	3.84	34.6	565	0.246	0.269	20.0	5.38	- 4.5
4.01	3.83	24.7	563	0.178	0.195	27.0	5.25	8.0
4.00	3.82	19.8	564	0.143	0.157	31.6	4.95	12
4.54	4.31	116	573	0.623	0.695	10.0	6.95	-19.5
4.53	4.30	89.6	573	0.483	0.539	12.2	6.57	-23
4.53	4.30	59.7	568	0.327	0.365	16.4	5.98	-19
4.53	4.30	39.6	565	0.218	0.243	22.3	5.42	-12
4.52	4.29	29.8	564	0.166	0.185	≈28	≈5.2	- 3.5
4.50	4.27	19.7	563	0.111	0.124	≈38	≈4.7	8.0
5.04	4.75	150	646	0.532	0.612	13.8	8.44	-18
5.06	4.77	120	644	0.420	0.483	15.8	7.63	-14
5.05	4.76	101	645	0.354	0.407	17.5	7.12	-17
5.05	4.78	79.9	646	0.281	0.323	20.2	6.53	-13.5
5.04	4.75	59.9	645	0.212	0.244	25.2	6.14	-12
5.02	4.73	40.2	616	0.154	0.177	31.2	5.53	- 2.5
5.00	4.71	29.9	600	0.120	0.138	37.0	5.11	6.5
5.00	4.71	24.9	602	0.100	0.115	≈44	5.06	14.5

\* $x_t$  Determined from Surface Probe Peak Pressure

**TABLE III**  
**SOURCE AND RANGE OF DATA USED IN THE TRANSITION REYNOLDS NUMBER**  
**CORRELATION (FIG. 10)**

Source	Symbol	$M_\infty$	$M_0$	$h \times 10^3$	$\theta_c$ , deg	$(R_x/in)_\infty \times 10^{-6}$	Tunnel	Test Section Size	Method of Transition Detection	Amount of Adjustment	$x_m$ , in	$T_w/T_{aw}$	$T_w/T_u$	Method of $x^*$ Determination
Present Study		3 3.5 4 4.55	2.8 3.4 3.8 4.3	5 (Sharp)	5	0.15 to 0.4	AEDC - VKF D	12 by 12 in	Maximum Probe Pressure	No Adjustment	44	$\approx 1.0$	0.80	Experimental Data $x_F = 56$ in. Ref. 20
Present Study		3 4 4.5 5	2.0 3.8 4.1 4.7 5.5	5 (Sharp)	5	0.15 to 0.5	AEDC - VKF A	40 by 40 in	Maximum Probe Pressure	No Adjustment	216	$\approx 1.0$	$\approx 0.90$	Experimental Data $x_F = 200$ to Ref. 9 and 28
Ref. 10 and VKF		8 8 8	5.5 7.0 8.4	Sharp	8	0.16 to 0.43	AEDC - VKF B	50-in Diam	Shadowgraph	1.08	245	0.72	0.63	VKF Experimental Data and Ref. 30 $x_F = 244$ in
Ref. 33		10	8.5	Sharp	6	0.13	AFRC - VKF C	50-in Diam	Maximum q	No Adjustment	$\approx 300$	$\approx 0.29$	$\approx 0.25$	VKF Experimental Data, $x_F = 300$ in
Ref. 10		18	7.5	Sharp	9	0.17	AEDC - VKF C	50-in Diam	Shadowgraph	1.1	$\approx 300$	$\approx 0.77$	$\approx 0.60$	
Ref. 11		14.2	9.1	4 (Sharp)	9	0.12, 0.2	AEDC - VKF F (Hotshot)	54-in Diam	Maximum q	No Adjustment	350	$\approx 0.22$	$\approx 0.19$	Ref. 32, $x_F = 304$ in
Ref. 10		6 8	5.0 8.2	Sharp	10	0.34 to 1.2	AEDC - VKF E	12 by 12 in	Shadowgraph	1.1 1.1	$\approx 64$ 1	$\approx 0.06$ $\approx 0.5$	$\approx 0.73$ $\approx 0.5$	Estimated Using $\delta^*$ $x_F = 54$ in
Ref. 34		10.2	5.2	4 to 10 (Sharp)	3.75	0.10 to 0.18	NASA - Langley	31 by 31-in Hypersonic	Maximum q	No Adjustment	158	0.43 to 0.63	0.37 to 0.54	Correlation Refs. 8 or 9 $x_F = 158$ in
Ref. 15	X	3.1	3.0	6 (Sharp)	5	0.1 to 0.67	NACA - Lewis	12 by 12 in	Maximum $T_w$	1.18	$\approx 40$	$\approx 1.0$	$\approx 0.00$	$x_F = 47$ in
Ref. 16	+	5.0	4.9	3 (Sharp)	2.5	0.16 to 0.47	NASA - Lewis	12 by 12 in	Maximum $T_w$	1.13	$\approx 47$	$\approx 1.0$	$\approx 0.00$	$x_F = 55$ in
Ref. 35		3.84	3.84	5 (Sharp)	5	0.18 to 0.48	IP1 - SWT	0 by 12 in	Maximum $T_w$	1.10	$\approx 49$	$\approx 1.0$	$\approx 0.80$	Experimental Data Ref. 31, $x_F = 48$ in

\*Adjustment for Method of Detection Based on Refs. 13 and 14

\*\*Cool-Wall Model

†Nitrogen Test Gas

**TABLE IV**  
**ESTIMATED CONE-PLANAR TRANSITION RATIOS**

1	2		3	4	5	6 $1 + 2 \left( \frac{\theta}{\theta_0} \right)$	7 $1 + 2 \left( \frac{\theta}{\theta_0/2} \right)$
	Free-Stream Conditions		Experimental (Fig. 11)	Theoretical (Ref. 22)	Critical Reynolds Number from Stability Experiments Ref. 12	Estimated, Eq. (7)	Estimated, Eq. (7) with Adjustments
Tunnel	$M_\infty$	$(Re/ln.)_\infty \times 10^{-6}$	$(Re)_\delta, \text{planar} \times 10^{-6}$	$(Re)_\delta, \text{planar-minimum} \times 10^{-6}$		$\frac{(Re)_\delta, \text{conc.}}{(Re)_\delta, \text{planar}}$	
D	3	0.2	1.42	0.016	$\approx 0.08$	1.022	1.23
A	3		2.25	0.016	$\approx 0.08$	1.014	1.14
16S	3		3.35	0.016	$\approx 0.08$	1.010	1.10
D	5		2.05	0.044	$\approx 0.5$	1.042	1.98
A	5		2.95	0.044	$\approx 0.5$	1.030	1.68
B	8		6.15	0.145		1.048	

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13. ABSTRACT An experimental investigation of laminar boundary-layer transition on a sharp, 10-deg total-angle, insulated cone at zero yaw was conducted in the AEDC-VKF 12- and 40-in. supersonic wind tunnels at free-stream Mach numbers from 3 to 6. This research was directed toward defining the relationship between the aerodynamic noise disturbances and boundary-layer transition Reynolds numbers $(Re_t)_\delta$ in high-speed wind tunnels and has extended previously published planar results to include axisymmetric models. A significant increase in $(Re_t)_\delta$ with increasing tunnel size (similar to the planar results) is shown to exist. Sharp cone transition Reynolds numbers from ten facilities (12- to 54-in.) for free-stream Mach numbers from 3 to 14 and a unit Reynolds number per inch range from $0.1 \times 10^6$ to $1.2 \times 10^6$ have been correlated using aerodynamic-noise-transition parameters. A quantitative correlation of the ratio between cone and planar $(Re_t)_\delta$ values has been developed which demonstrates a strong Mach number dependence and also indicates a variation with tunnel size and unit Reynolds number.			

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